

# CONSIDER A SPHERICAL EARTH HEAT CAPACITY, TIME CONSTANT AND SENSITIVITY OF EARTH'S CLIMATE SYSTEM

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Topics in Atmospheric and Oceanic Sciences Seminar



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<http://www.ecd.bnl.gov/steve>

# Consider a Spherical Cow

A Course in Environmental Problem Solving

JOHN HARTE



longer, directional force  
resisting  
downward motion

mg = symmetrical  
force downward



$2.469 \times 10^{21}$   $m = -21 - 222$



# OVERVIEW

Earth 's energy balance and perturbations

Climate sensitivity – definition, importance, past and current estimates

Climate sensitivity from paleoclimate

Uncertainty in aerosol forcing and its implications

Empirical climate sensitivity from temperature change over the instrumental record

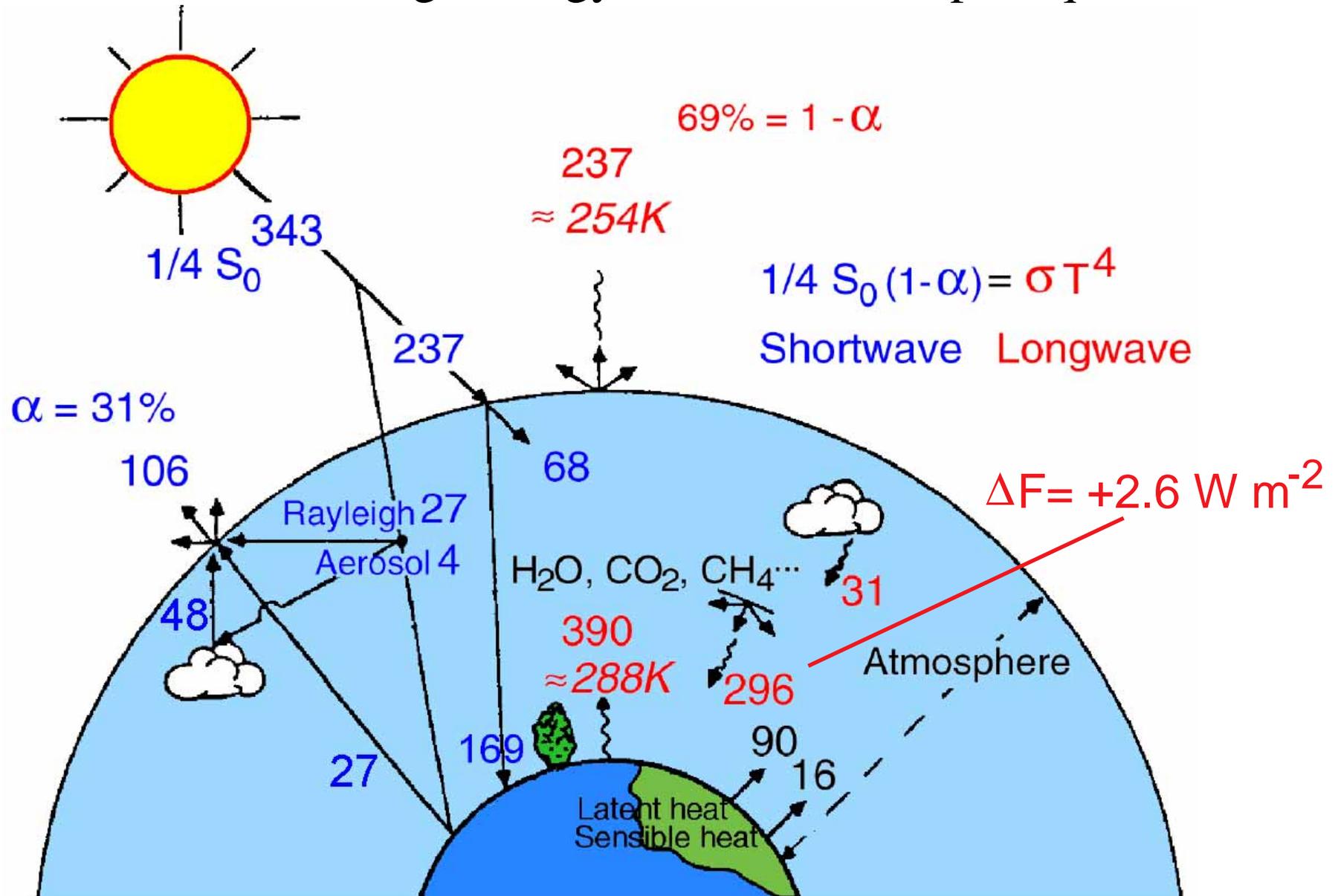
Climate sensitivity from climate models

Climate sensitivity from whole-earth energy-balance models

Concluding remarks

# GLOBAL ENERGY BALANCE

Global and annual average energy fluxes in watts per square meter



Schwartz, 1996, modified from Ramanathan, 1987

# ***ATMOSPHERIC RADIATION***

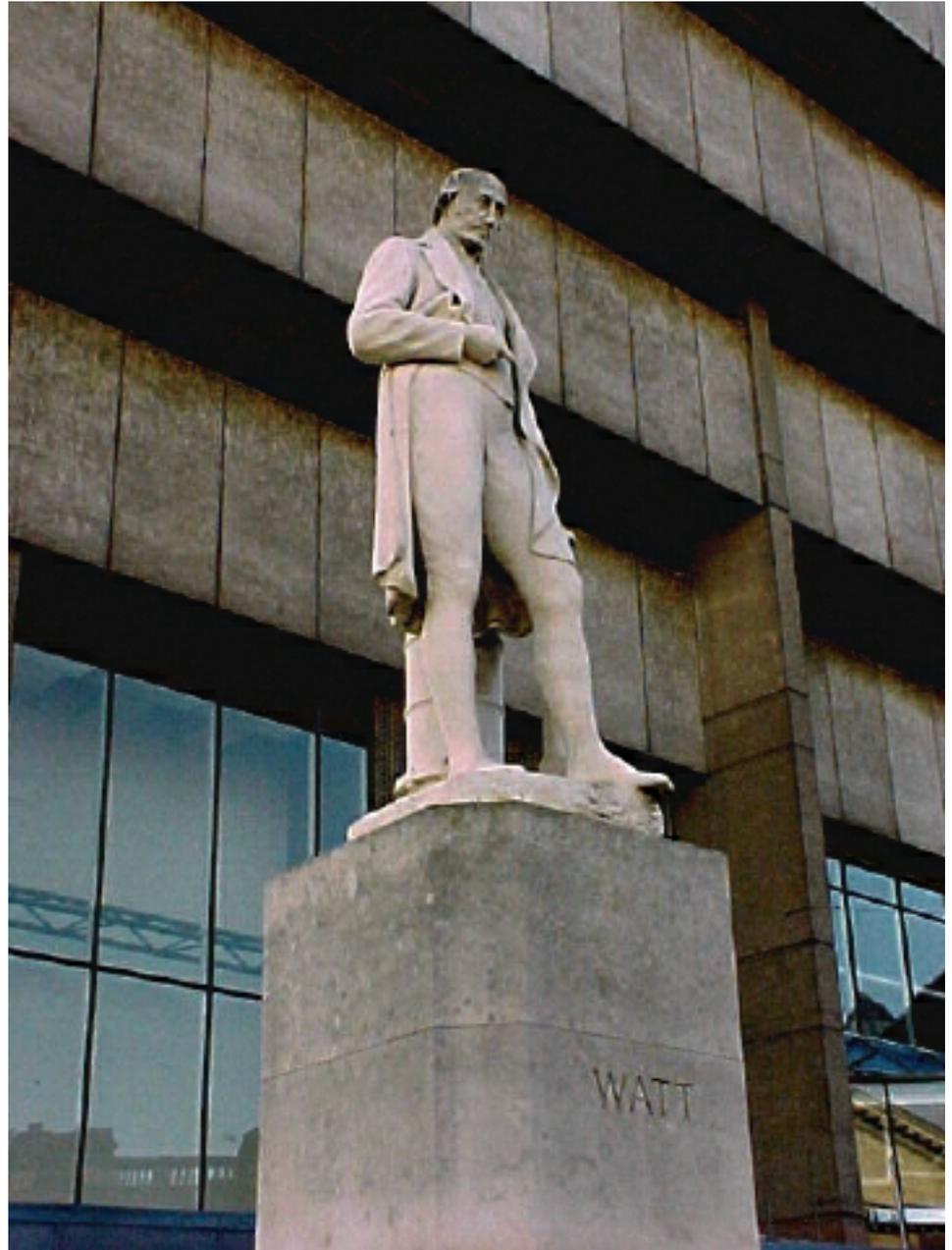
*Energy per area per  
time*

*Power per area*

*Unit:*

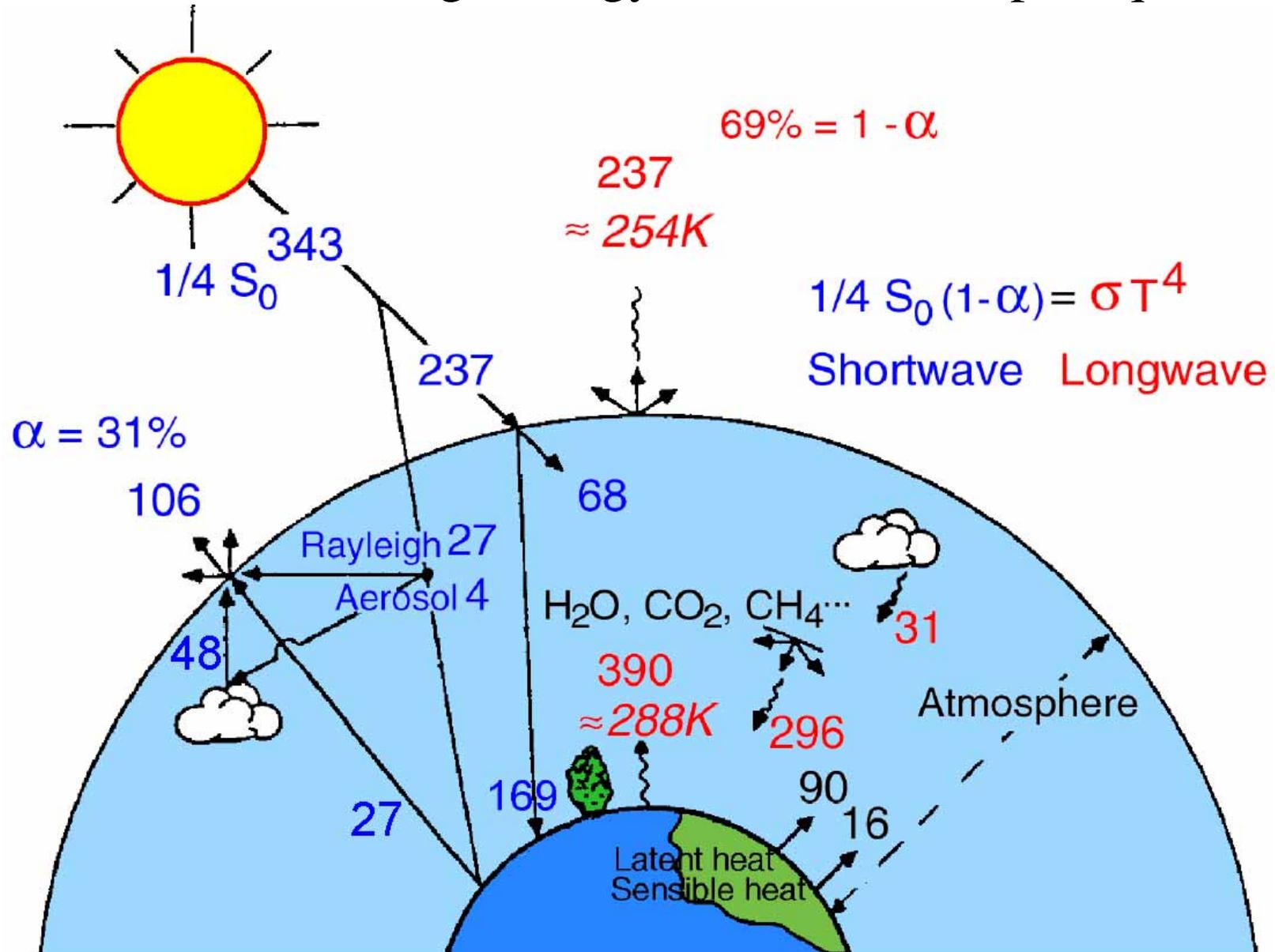
*Watt per square meter*

*$W m^{-2}$*



# GLOBAL ENERGY BALANCE

Global and annual average energy fluxes in watts per square meter



*Schwartz, 1996, modified from Ramanathan, 1987*

# ***RADIATIVE FORCING***

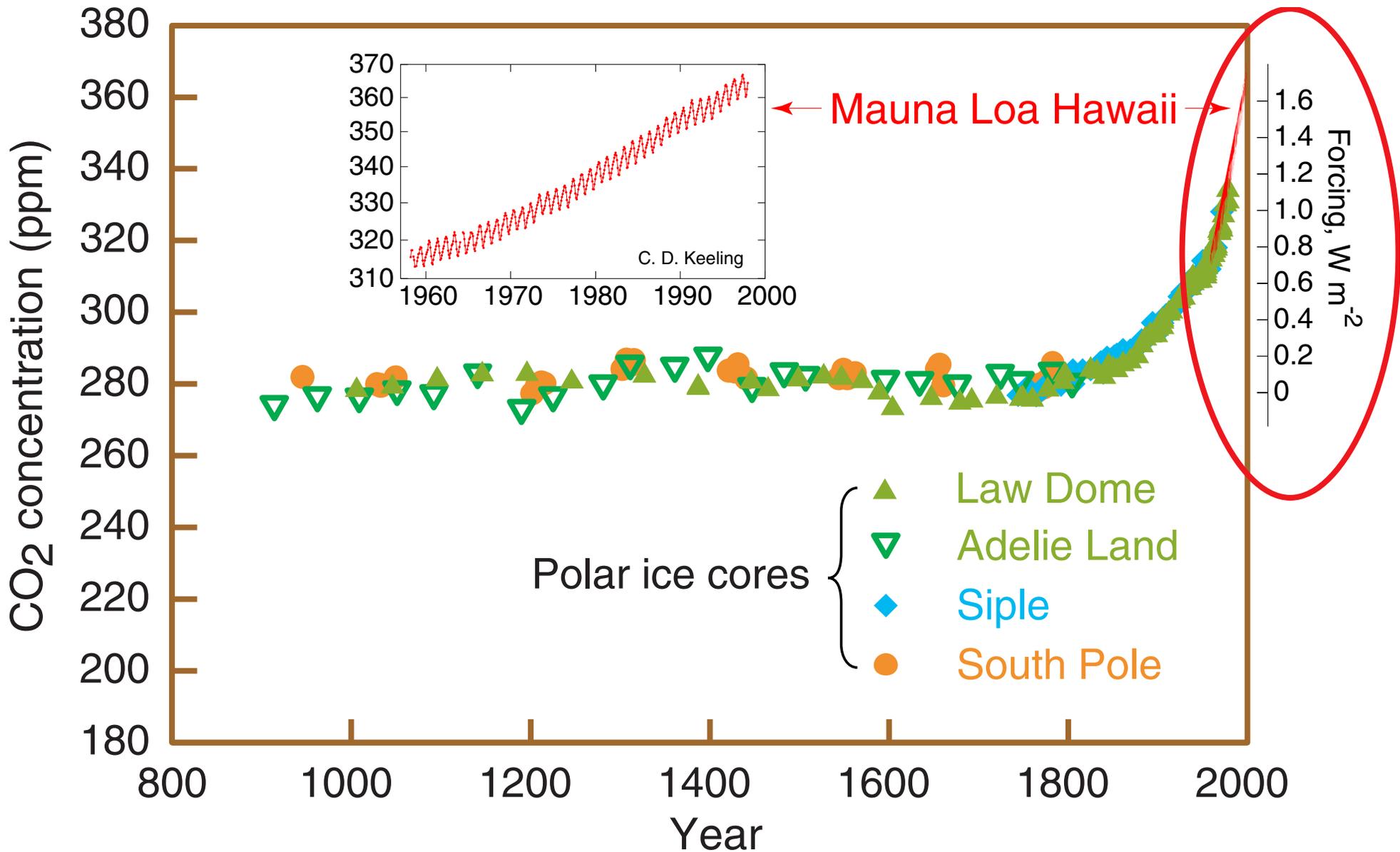
A *change* in a radiative flux term in Earth's radiation budget,  $\Delta F$ ,  $\text{W m}^{-2}$ .

## ***Working hypothesis:***

*On a global basis radiative forcings are additive and fungible.*

- This hypothesis is fundamental to the radiative forcing concept.
- This hypothesis underlies much of the assessment of climate change over the industrial period.

# ATMOSPHERIC CARBON DIOXIDE IS INCREASING



Global carbon dioxide concentration and infrared radiative forcing over the last thousand years

# ***CLIMATE RESPONSE***

The *change* in global and annual mean temperature,  $\Delta T$ , K, resulting from a given radiative forcing.

***Working hypothesis:***

*The change in global mean temperature is proportional to the forcing, but independent of its nature and spatial distribution.*

$$\Delta T = S \Delta F$$

# *CLIMATE SENSITIVITY*

The *change* in global and annual mean temperature per unit forcing,  $S$ ,  $\text{K}/(\text{W m}^{-2})$ ,

$$S = \Delta T / \Delta F.$$

Climate sensitivity is not known and is the objective of much current research on climate change.

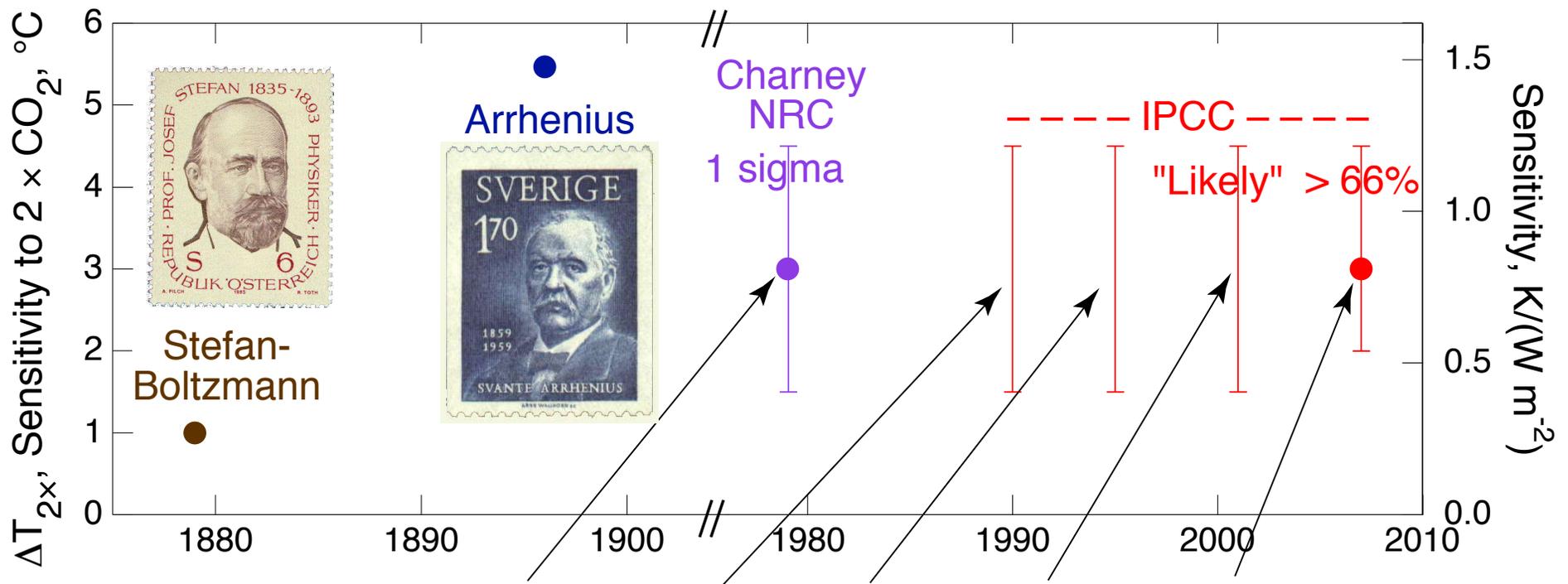
Climate sensitivity is often expressed as the temperature for doubled  $\text{CO}_2$  concentration  $\Delta T_{2\times}$ .

$$\Delta T_{2\times} = S \Delta F_{2\times}$$

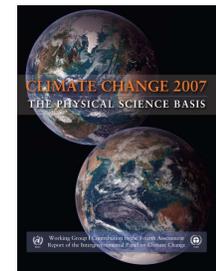
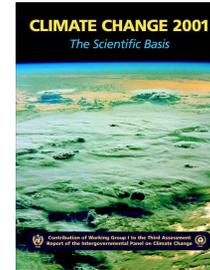
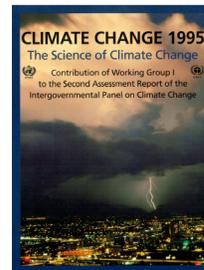
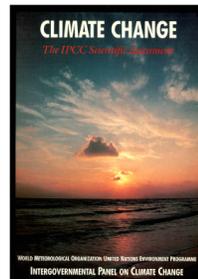
$$\Delta F_{2\times} \approx 3.7 \text{ W m}^{-2}$$

# CLIMATE SENSITIVITY ESTIMATES THROUGH THE AGES

Estimates of central value and uncertainty range from major national and international assessments



**Carbon Dioxide and Climate:  
A Scientific Assessment**  
NATIONAL ACADEMY OF SCIENCES  
Washington, D.C. 1979



Despite extensive research, climate sensitivity remains *highly uncertain*.

# *IMPLICATIONS OF UNCERTAINTY IN CLIMATE SENSITIVITY*

Uncertainty in climate sensitivity translates directly into . . .

- Uncertainty in the amount of *incremental atmospheric CO<sub>2</sub>* that would result in a given increase in global mean surface temperature.
- Uncertainty in the amount of *fossil fuel carbon* that can be combusted consonant with a given climate effect.

*At present this uncertainty is about a factor of 3.*

# ***IMPORTANCE OF KNOWLEDGE OF CLIMATE TO INFORMED DECISION MAKING***

- The lifetime of incremental atmospheric CO<sub>2</sub> is about 100 years.
- The expected life of a new coal-fired power plant is 50 to 75 years.

***Actions taken today will have long-lasting effects.***

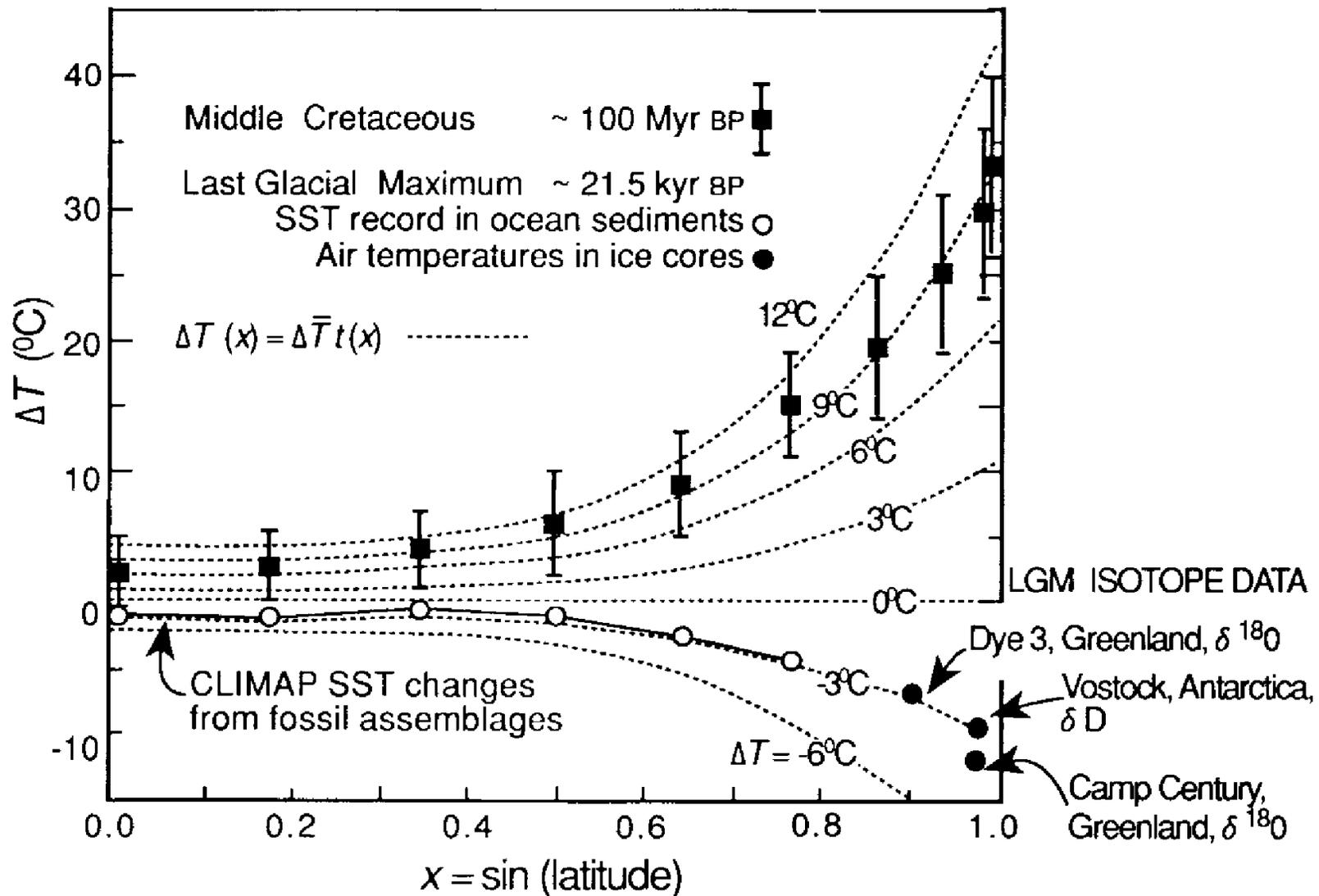
***Early knowledge of climate sensitivity can result in huge averted costs.***

# ***KEY APPROACHES TO DETERMINING CLIMATE SENSITIVITY***

- ***Paleoclimate studies***: Forcing and response over time scales from millennial to millions of years.
- ***Empirical***: Forcing and response over the instrumental record.
- ***Climate modeling***: Understanding the processes that comprise Earth's climate system and representing them in large-scale numerical models.

# CLIMATE SENSITIVITY FROM PALEOCLIMATE

# GLOBAL MEAN TEMPERATURE FROM PALEO DATA



*Hoffert & Covey, Nature, 1992*

Last Glacial Maximum:  $\Delta T = -3$  K; Middle Cretaceous,  $\Delta T = +9$  K.

# CLIMATE SENSITIVITY FROM PALEO DATA

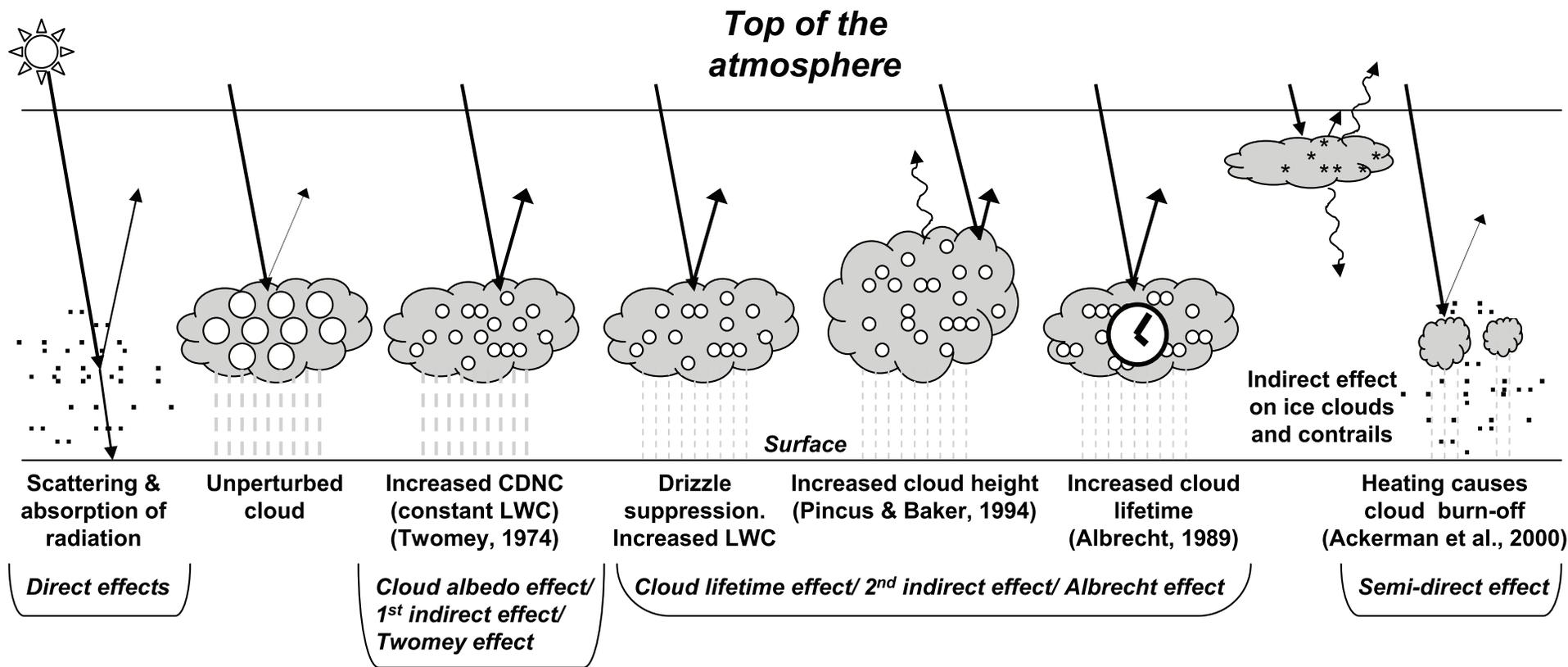
Component	Last Glacial Maximum	Middle Cretaceous
Forcing, $\text{W m}^{-2}$	Value $\pm 1 \sigma$	Value $\pm 1 \sigma$
Sun	$0.0 \pm 0.2$	$-1.2 \pm 0.2$
Albedo	$-3.0 \pm 0.5$	$5.8 \pm 0.9$
Greenhouse	$-2.8 \pm 0.3$	$11.1 \pm 6.7$
Aerosol	$-0.9 \pm 0.7$	
Total $\Delta F$ , $\text{W m}^{-2}$	$-6.7 \pm 0.9$	$15.7 \pm 6.8$
$\Delta T$ , K	$-3.0 \pm 0.5$	$9.0 \pm 2.0$
$S$ , $\text{K}/(\text{W m}^{-2})$	$0.45 \pm 0.11$	$0.57 \pm 0.27$
$\Delta T_{2\times}$ , K ( $F_{2\times} = 4.4 \text{ W m}^{-2}$ )	$2.0 \pm 0.5$	$2.5 \pm 1.2$

*Hoffert & Covey, Nature, 1992*

Best estimate  $S = 0.51 \pm 0.2 \text{ K}/(\text{W m}^{-2})$ ;  $\Delta T_{2\times} = 2.3 \pm 0.9 \text{ K}$  ( $1 \sigma$ ).

# UNCERTAINTY IN AEROSOL FORCING AND ITS IMPLICATIONS

# AEROSOL INFLUENCES ON CLOUDS AND RADIATION

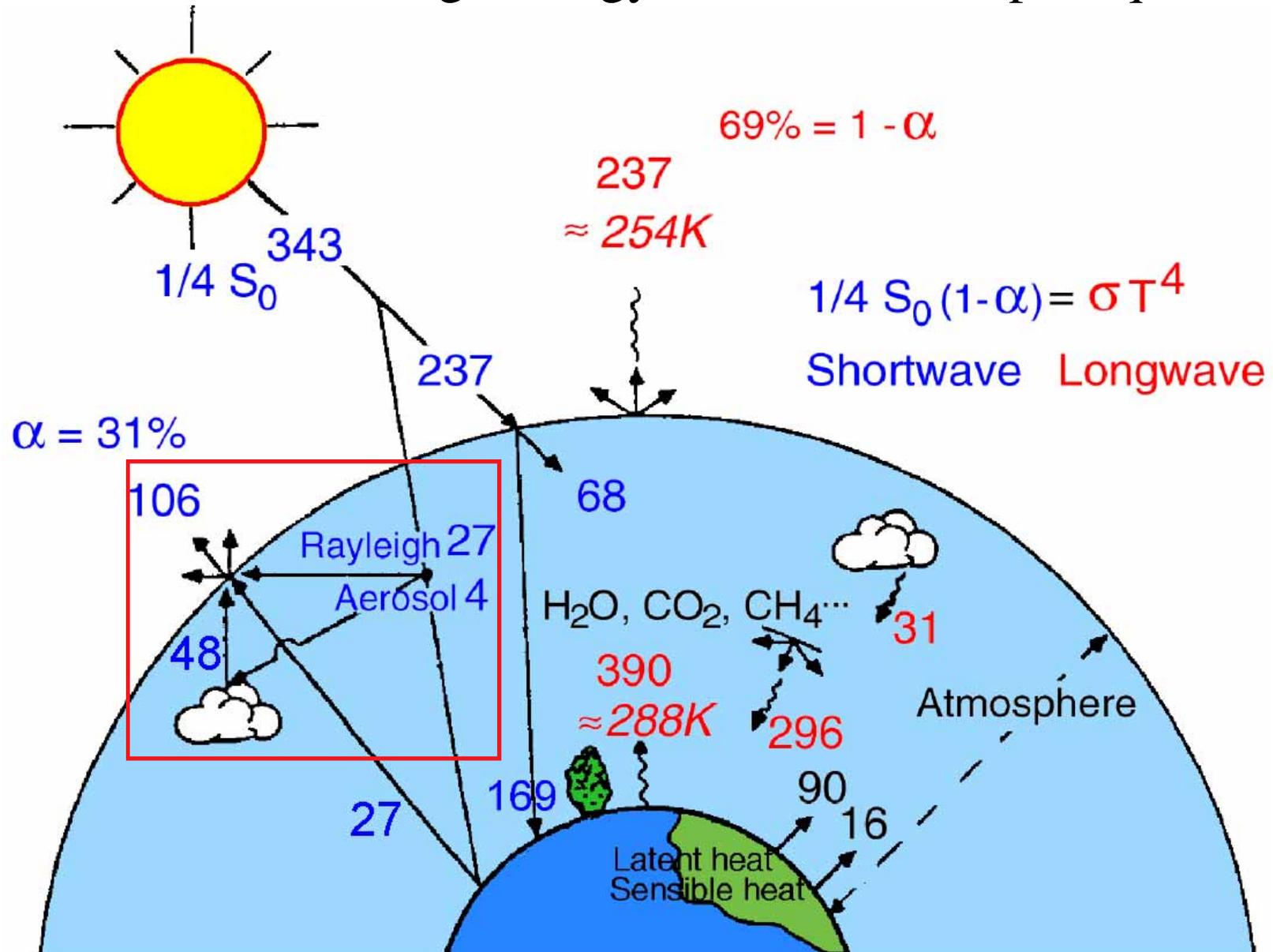


IPCC, AR4, 2007

Aerosol radiative forcing is a *change* in atmospheric radiation budget due to the change in amount or properties of aerosols, typically taken as present aerosol vs. preindustrial aerosol.

# GLOBAL ENERGY BALANCE

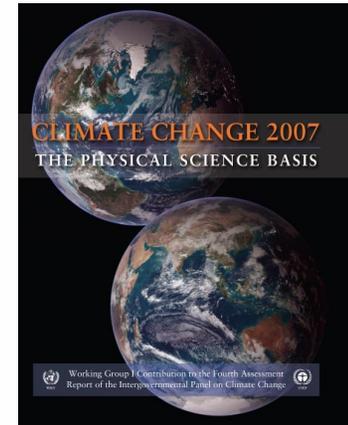
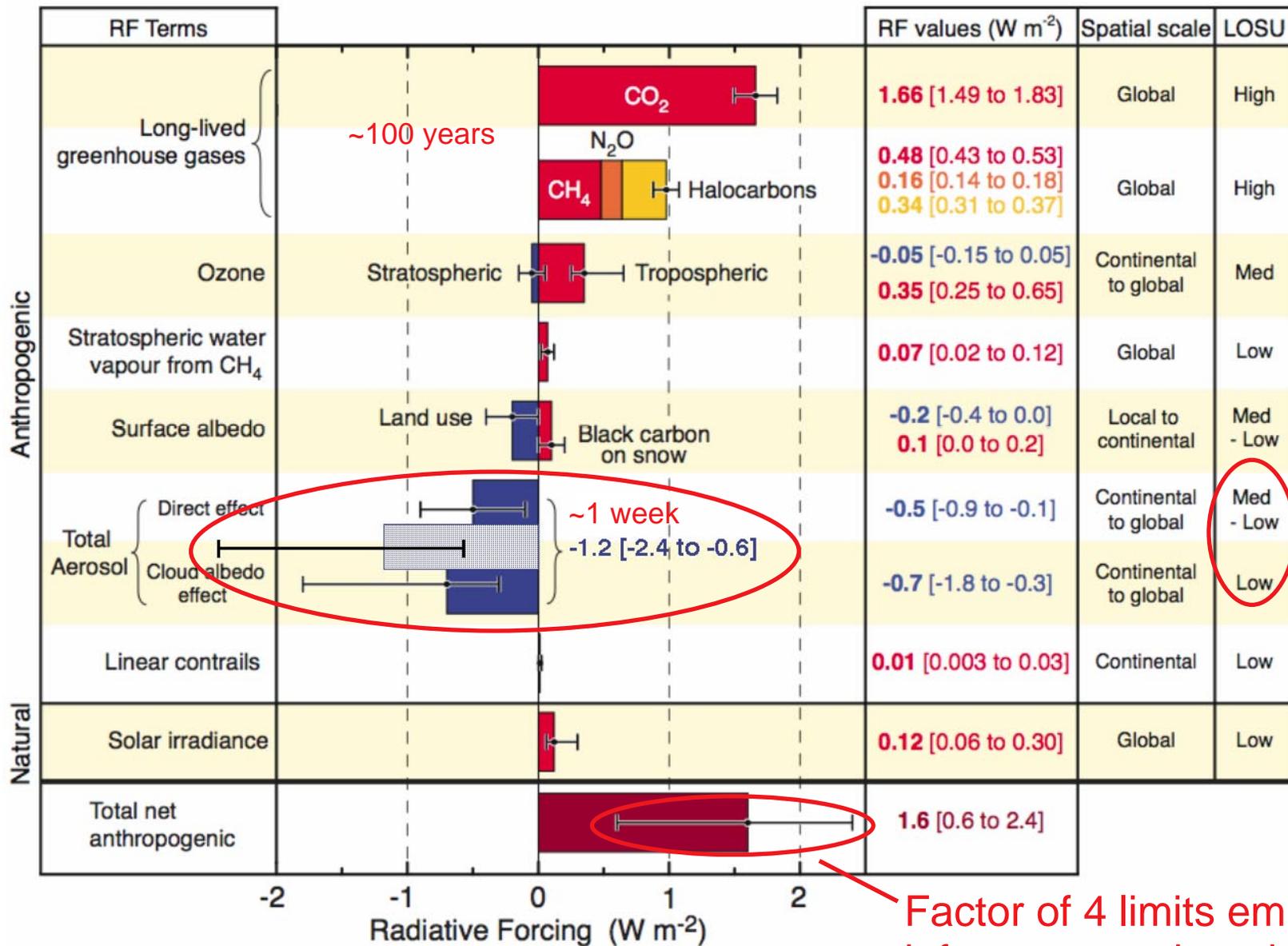
Global and annual average energy fluxes in watts per square meter



*Schwartz, 1996, modified from Ramanathan, 1987*

# GLOBAL-MEAN RADIATIVE FORCINGS (RF)

Pre-industrial to present (Intergovernmental Panel on Climate Change, 2007)



©IPCC 2007: WG1-AR4

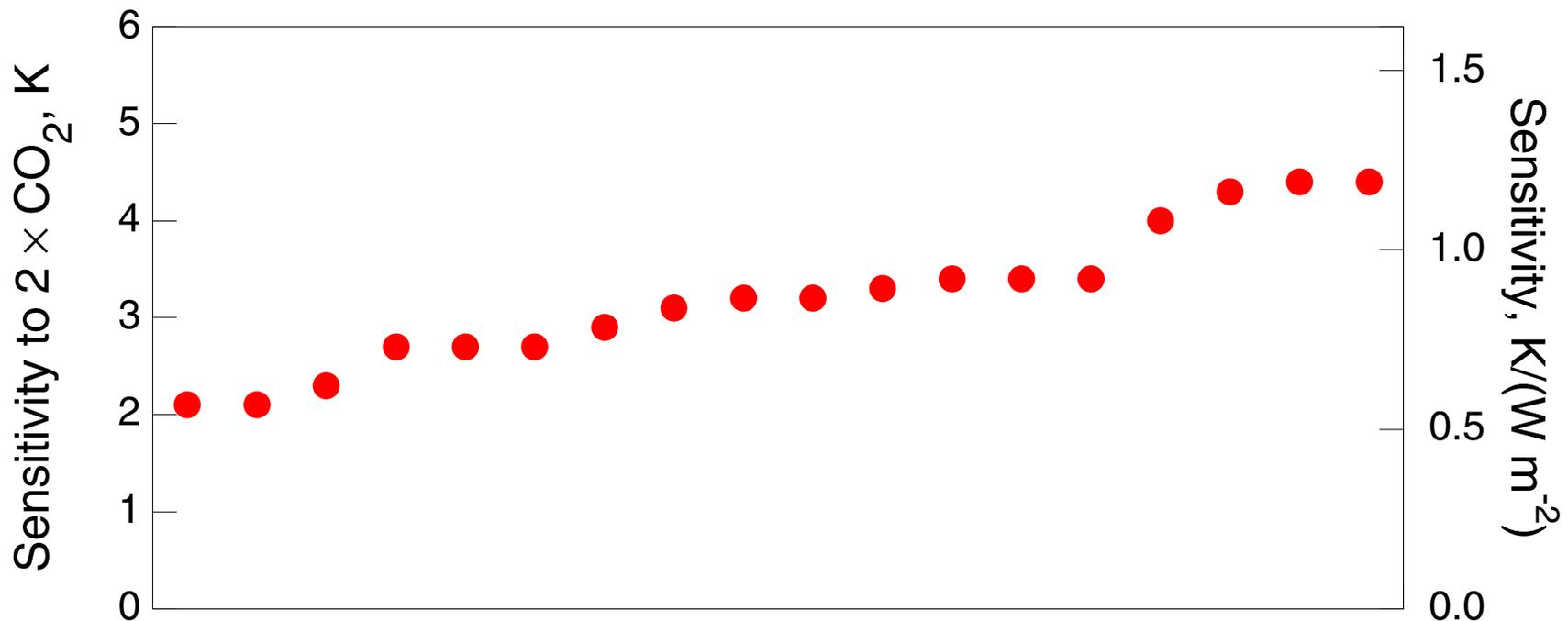
Factor of 4 limits empirical inferences and model evaluation.

LOSU denotes level of scientific understanding.

# CLIMATE SENSITIVITY FROM CLIMATE MODELS

# CLIMATE SENSITIVITY ESTIMATES FROM GLOBAL CLIMATE MODELS

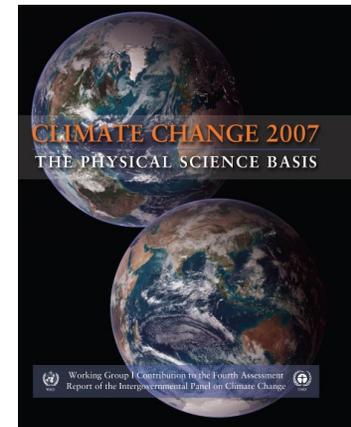
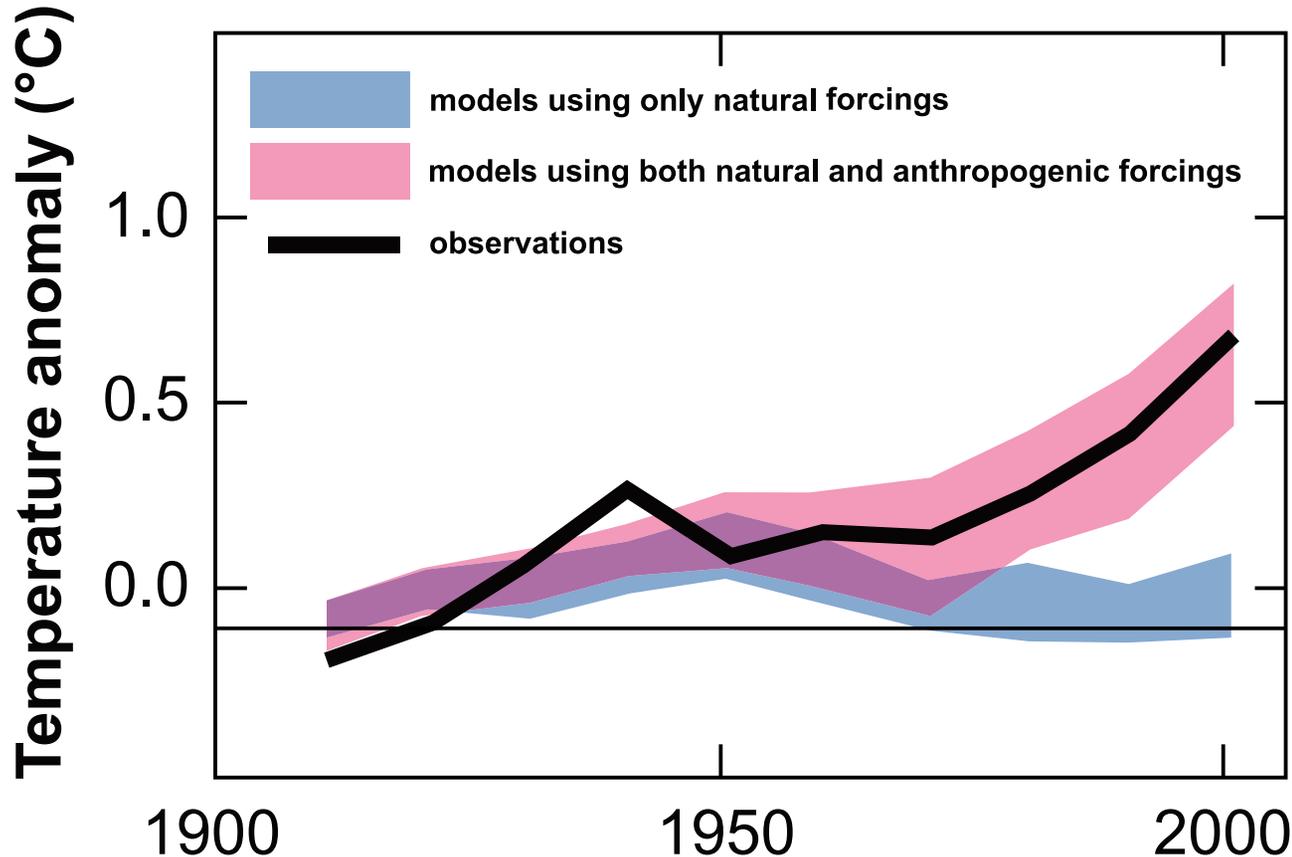
18 Current global climate models – IPCC AR4, 2007



*Range of model sensitivities is identical with range of current overall IPCC sensitivity estimate.*

# TOO ROSY A PICTURE?

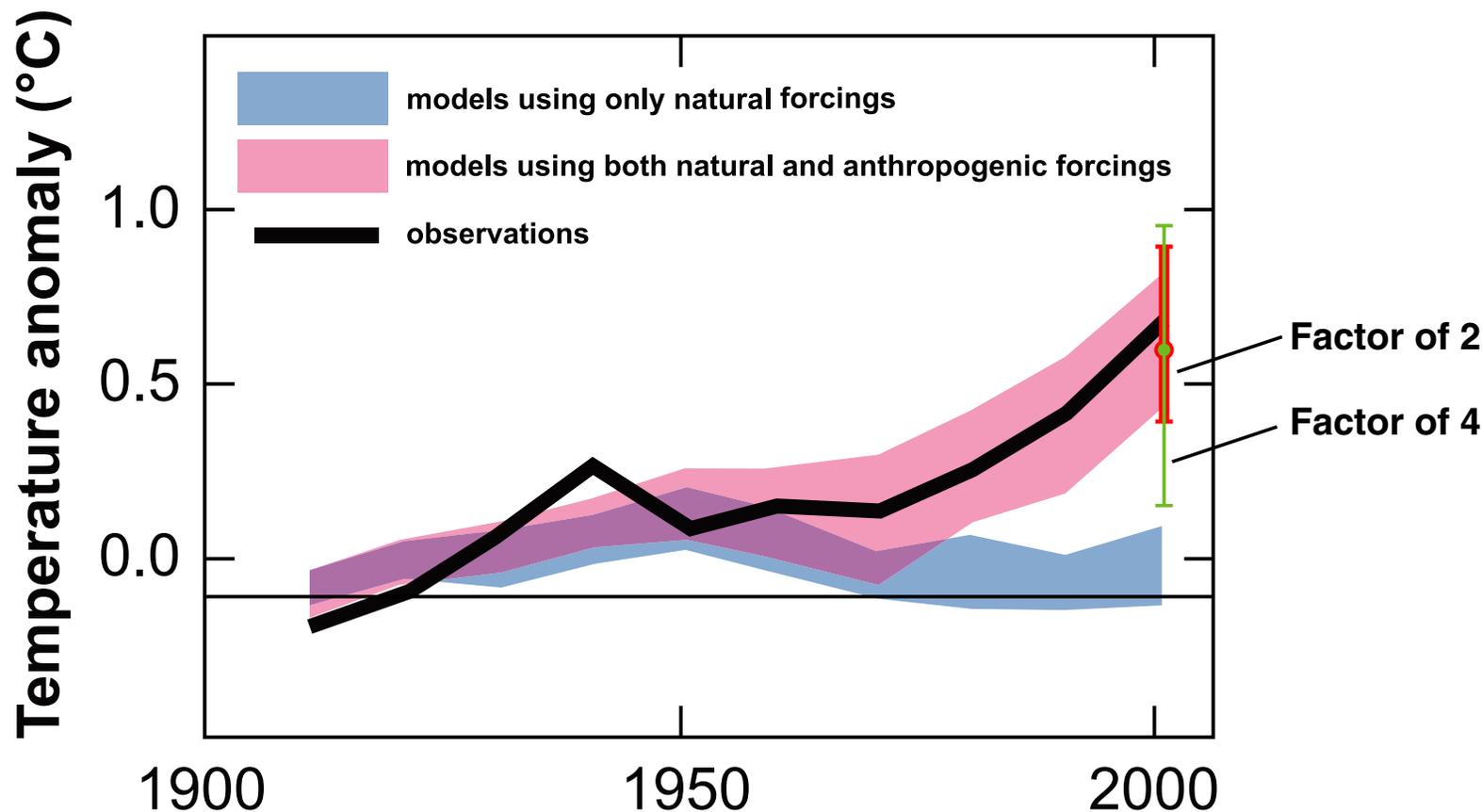
Ensemble of 58 model runs with 14 global climate models



- “ Simulations that incorporate anthropogenic forcings, including increasing greenhouse gas concentrations and the effects of aerosols, and that also incorporate natural external forcings provide a *consistent explanation of the observed temperature record*.
- “ These simulations used models with *different climate sensitivities, rates of ocean heat uptake and magnitudes and types of forcings*.

# TOO ROSY A PICTURE?

Ensemble of 58 model runs with 14 global climate models



*Schwartz, Charlson & Rodhe, Nature Reports – Climate Change, 2007*

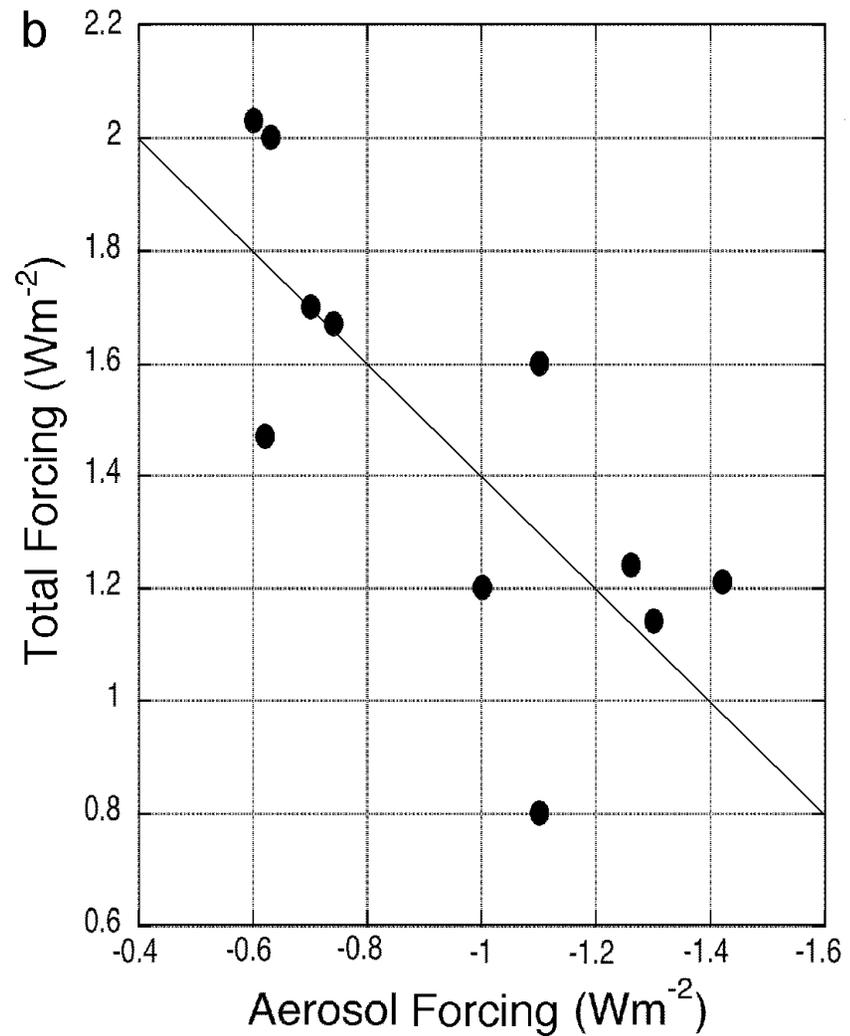
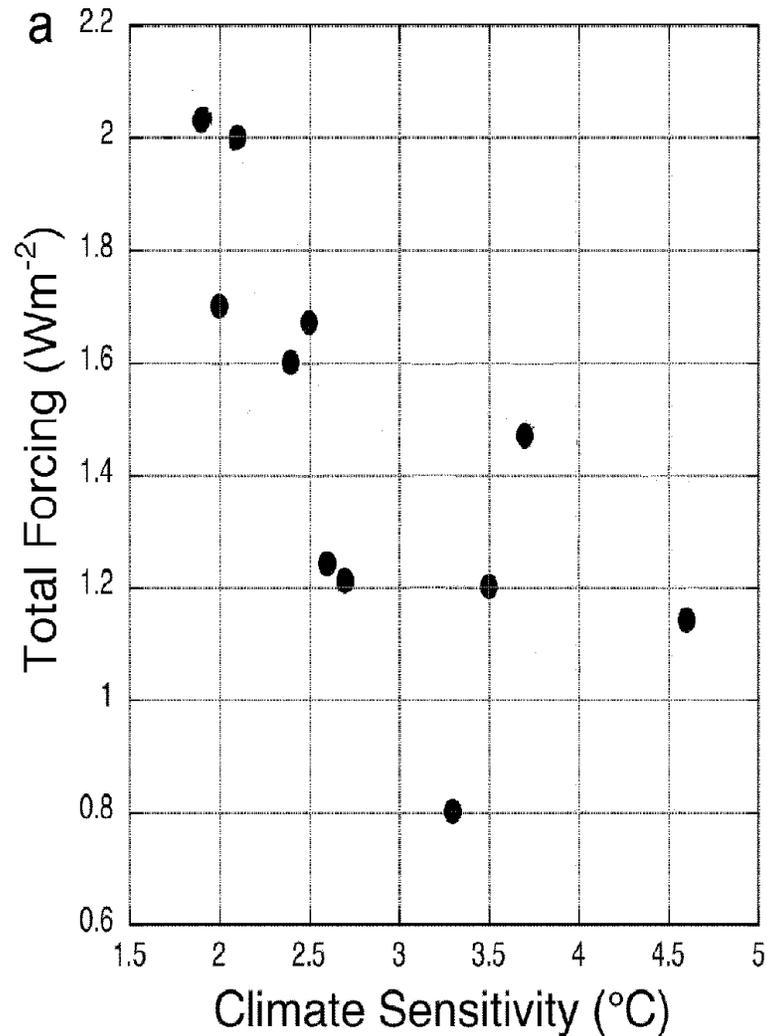
Uncertainty in modeled temperature increase – less than a factor of 2, red – is *well less than uncertainty in forcing* – a factor of 4, green.

The models *did not span the full range of the uncertainty* and/or . . .

The forcings used in the model runs were *anticorrelated with the sensitivities of the models*.

# CORRELATION OF AEROSOL FORCING, TOTAL FORCING, AND SENSITIVITY IN CLIMATE MODELS

Eleven models used in 2007 IPCC analysis



*Modified from Kiehl, GRL, 2007*

Climate models with higher sensitivity have lower total forcing.

EMPIRICAL  
CLIMATE SENSITIVITY  
FROM TEMPERATURE  
CHANGE OVER THE  
INSTRUMENTAL RECORD

# EMPIRICAL DETERMINATION OF CLIMATE SENSITIVITY OVER INDUSTRIAL PERIOD

Sensitivity is temperature change upon forcing accounting for transient heat uptake – *modified from Gregory et al. J. Clim. 2002*

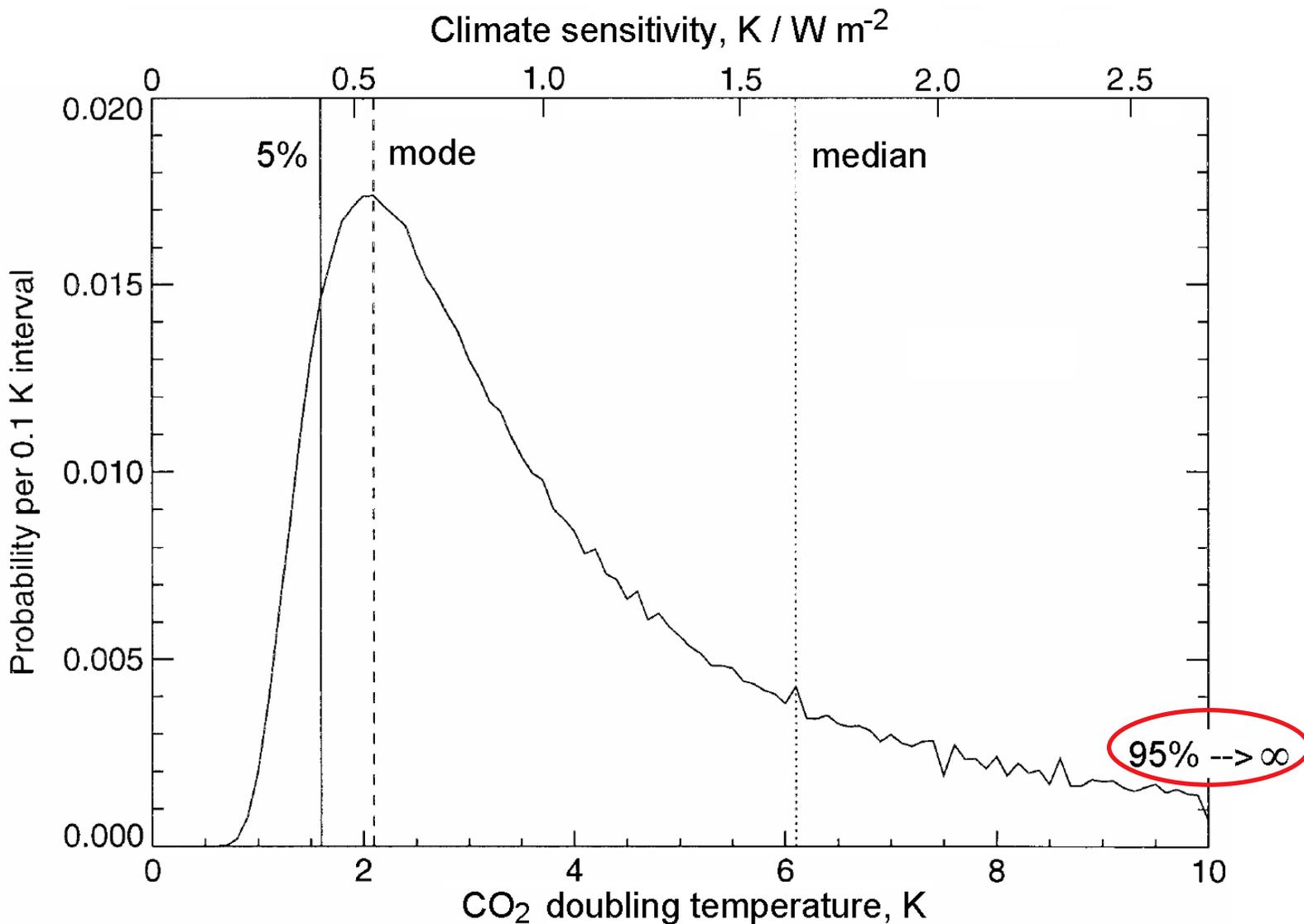
$$S = \frac{\Delta T}{\Delta F - (dH / dt)}$$

Evaluated for 1957-1994 vs. 1861-1900 for  $\Delta F_{2\times} = 3.71 \text{ W m}^{-2}$

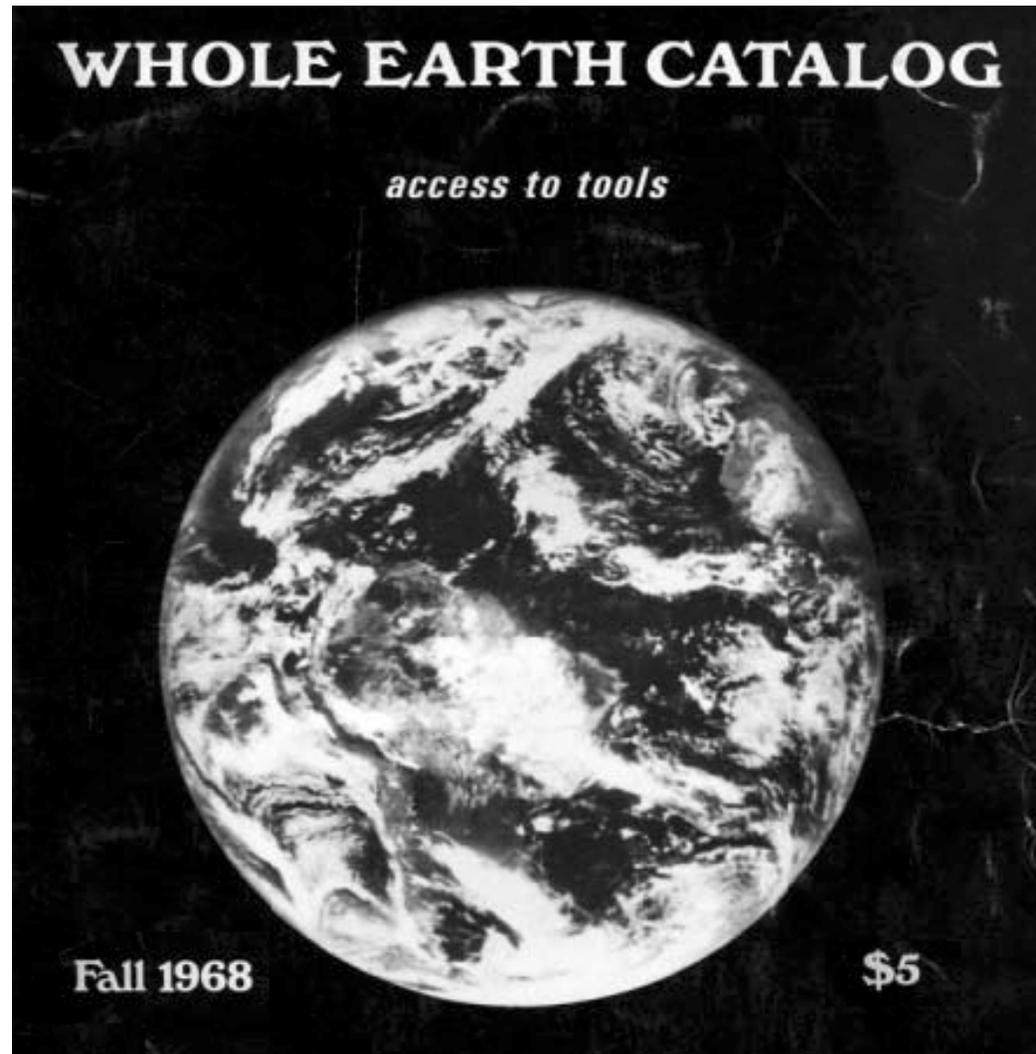
Symbol	Quantity	Value $\pm 1\sigma$	Unit
$\Delta T$	Temperature change	$0.335 \pm 0.017$	K
$\Delta F$	Forcing	$0.35 \pm 0.33$	$\text{W m}^{-2}$
$dH / dt$	Planetary heat uptake rate	$0.16 \pm 0.08$	$\text{W m}^{-2}$
$S$	Climate sensitivity	$0.56^{+2.2}_{-0.07}$	$\text{K}/(\text{W m}^{-2})$
$\Delta T_{2\times}$	$\Delta T$ for doubled $\text{CO}_2$	$2.1^{+8}_{-0.24}$	K

# EMPIRICAL DETERMINATION OF CLIMATE SENSITIVITY OVER INDUSTRIAL PERIOD

Probability distribution function for climate sensitivity



# CLIMATE SENSITIVITY FROM WHOLE EARTH ENERGY BALANCE MODELS



# ENERGY BALANCE MODEL OF EARTH'S CLIMATE SYSTEM



$$\text{Global energy balance: } C \frac{dT_s}{dt} = \frac{dH}{dt} = Q - E = \frac{\gamma J_S}{4} - \epsilon \sigma T_s^4$$

$C$  is heat capacity coupled to climate system on relevant time scale

$T_s$  is global mean surface temperature       $H$  is global heat content

$Q$  is absorbed solar energy

$E$  is emitted longwave flux

$J_S$  is solar constant

$\gamma$  is planetary co-albedo

$\sigma$  is Stefan-Boltzmann constant

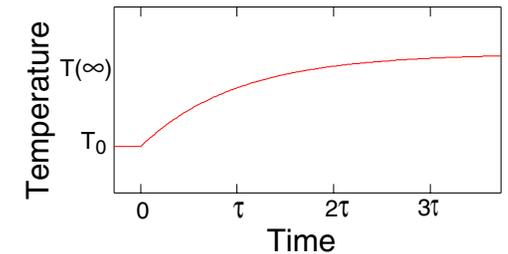
$\epsilon$  is effective emissivity

# ENERGY BALANCE MODEL OF EARTH'S CLIMATE SYSTEM



Apply step-function forcing:  $\Delta F = \Delta(Q - E)$

At new “equilibrium”  $\Delta T_s(\infty) = S\Delta F$



$S$  is equilibrium climate sensitivity  $S = \frac{T_0}{\gamma_0 J_S} \frac{1}{\left(1 - \frac{1}{4} \frac{d \ln \gamma}{d \ln T} \Big|_0 + \frac{1}{4} \frac{d \ln \epsilon}{d \ln T} \Big|_0\right)}$  K / (W m<sup>-2</sup>)

If  $\gamma$  and  $\epsilon$  are constant (*no feedbacks*),  $S = \frac{T_0}{\gamma_0 J_S}$  Stefan-Boltzmann sensitivity,  $S_{SB} = 0.30$  K / (W m<sup>-2</sup>);  $\Delta T_{2\times} = 1.1$  K

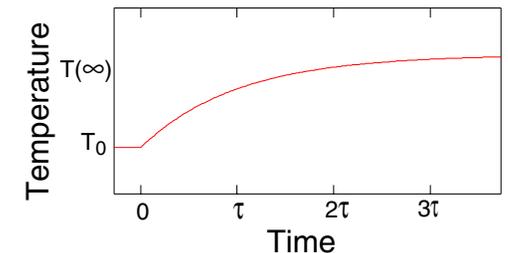
$f$  is feedback factor  $f = \frac{1}{\left(1 - \frac{1}{4} \frac{d \ln \gamma}{d \ln T} \Big|_0 + \frac{1}{4} \frac{d \ln \epsilon}{d \ln T} \Big|_0\right)} = \frac{1}{1 - \mathcal{F}}$   $\mathcal{F}$  is feedback strength

# ENERGY BALANCE MODEL OF EARTH'S CLIMATE SYSTEM



Apply step-function forcing:  $\Delta F = \Delta(Q - E)$

At “equilibrium”  $\Delta T_s(\infty) = S\Delta F$



$S$  is equilibrium climate sensitivity  $S = \frac{T_0}{\gamma_0 J_S} f = S_{\text{SB}} f$  Stefan-Boltzmann sensitivity times feedback factor

***Time dependence:***  $\Delta T_s(t) = S\Delta F(1 - e^{-t/\tau})$

$\tau$  is climate system time constant  $\tau = CS$  or  $S = \tau / C$

***One equation in three unknowns!***

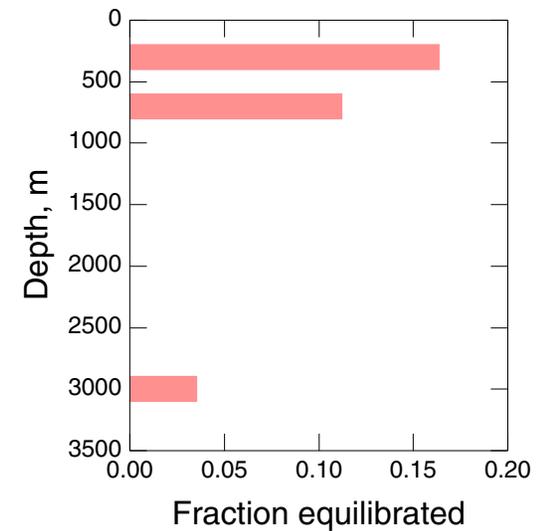
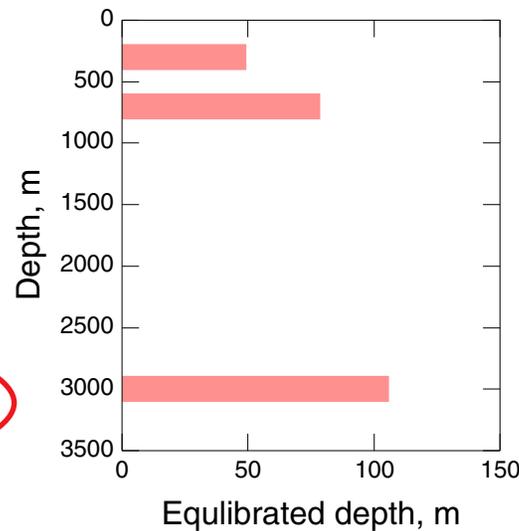
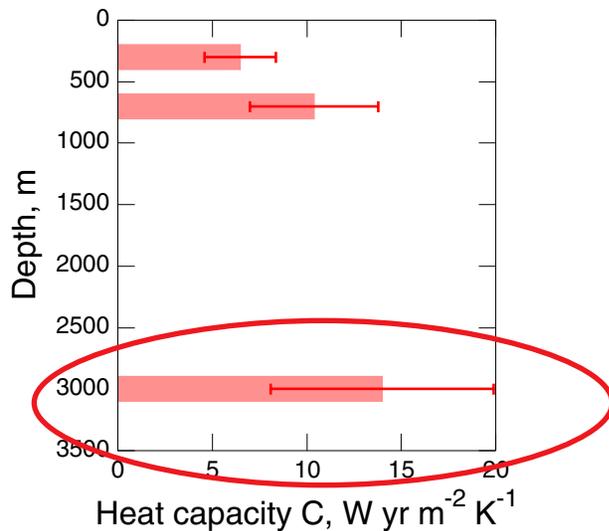
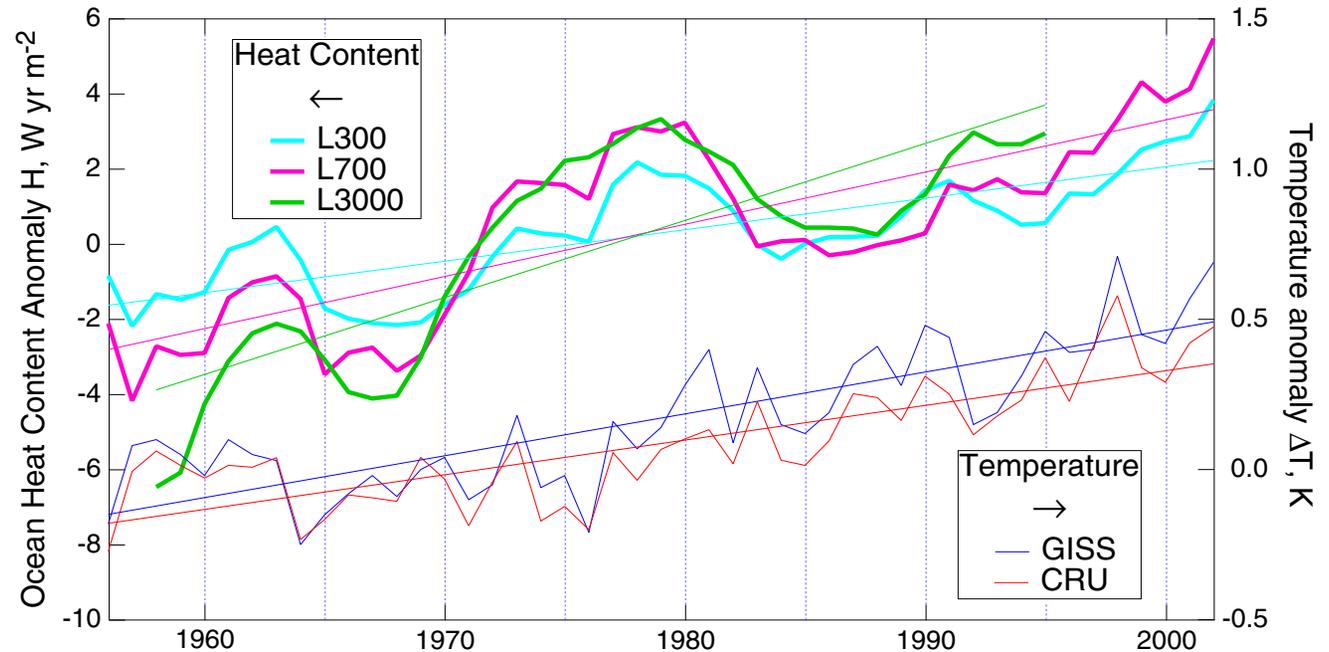
***Approach:*** Determine  $C$  and  $\tau$  from measurements; calculate sensitivity  $S$ .

# EMPIRICAL DETERMINATION OF OCEAN HEAT CAPACITY

$$C = \frac{dH / dt}{dT_s / dt}$$

Ocean heat content  
*H*: Levitus *et al.*,  
 GRL, 2005

Surface temperature  
*T<sub>s</sub>*: GISS, CRU

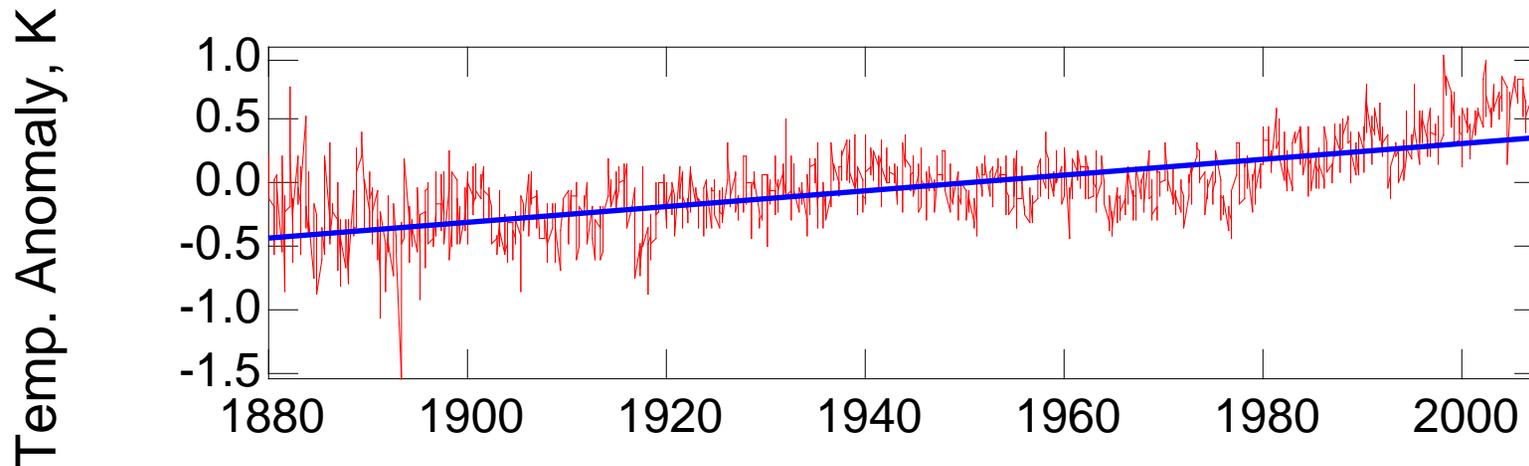


- ~50% of heat capacity is between surface and 300 m.
- Other heat sinks raise global heat capacity to  $17 \pm 7 \text{ W yr m}^{-2} \text{ K}^{-1}$ .

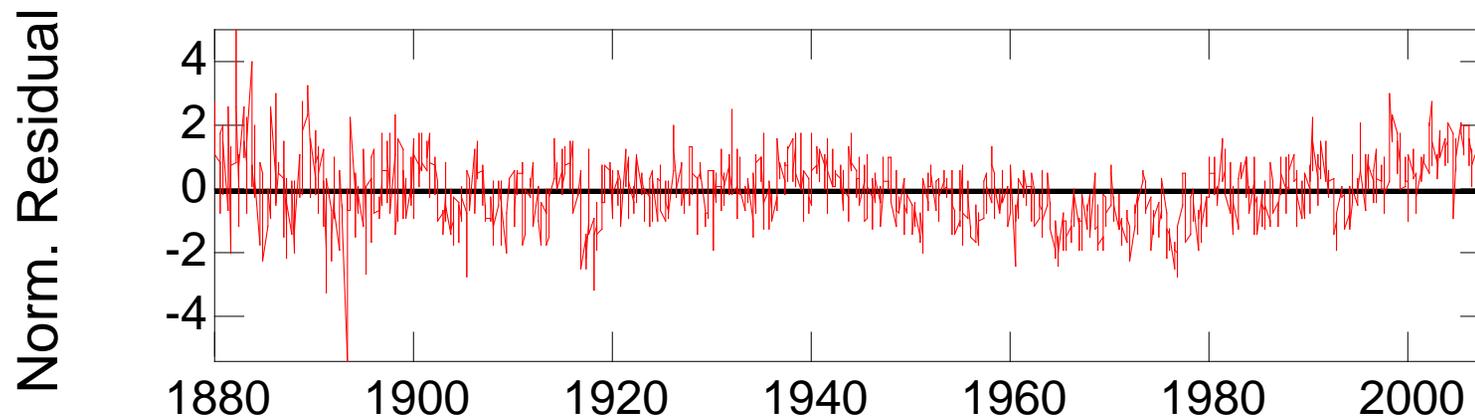
# TIME CONSTANT OF EARTH'S CLIMATE SYSTEM

## Determination from autocorrelation of time series

**Input:** Monthly global-mean surface temperature anomaly  $T_s$



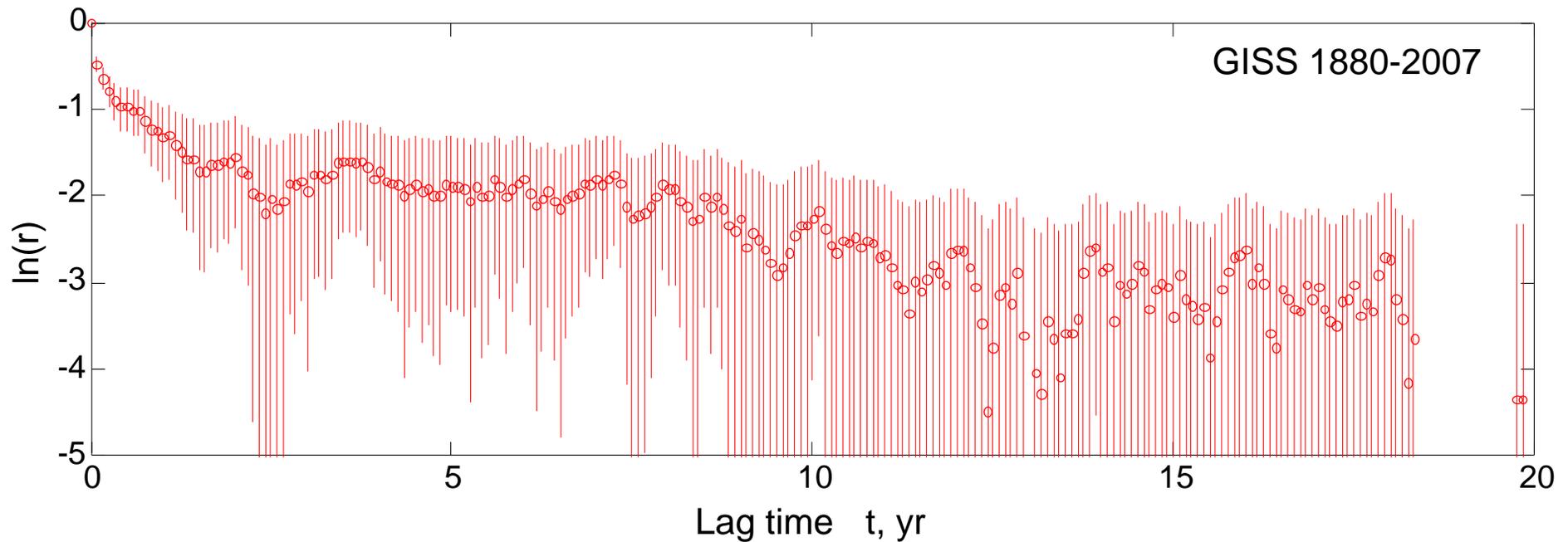
Remove long term trend; plot the residuals:



# TIME CONSTANT OF EARTH'S CLIMATE SYSTEM

## Determination from autocorrelation of time series (*cont'd*)

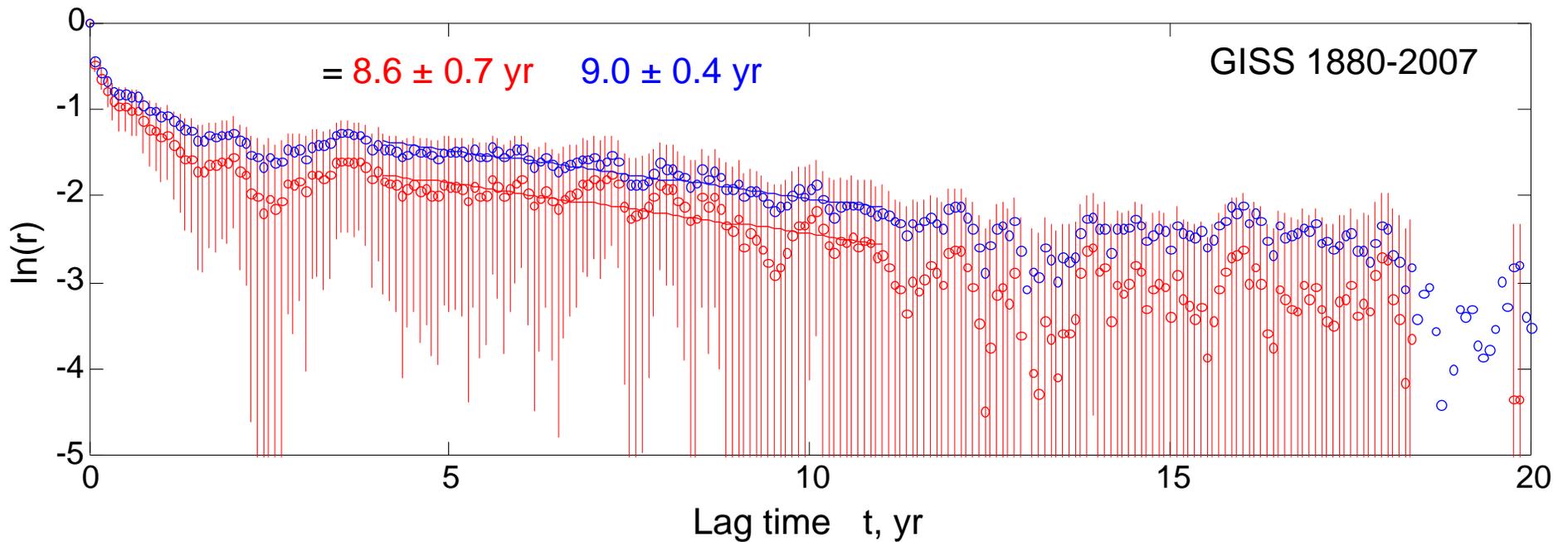
Calculate *autocorrelogram*  $r(t)$ , correlation coefficient of detrended time series with itself, lagged by  $t$  (& standard deviations).



# TIME CONSTANT OF EARTH'S CLIMATE SYSTEM

## Determination from autocorrelation of time series (*cont'd*)

Evaluate *climate system time constant* as  $\tau = (d \ln r(t) / d t)^{-1}$   
*Correct for short duration of time series.*



Summary (multiple data sets):

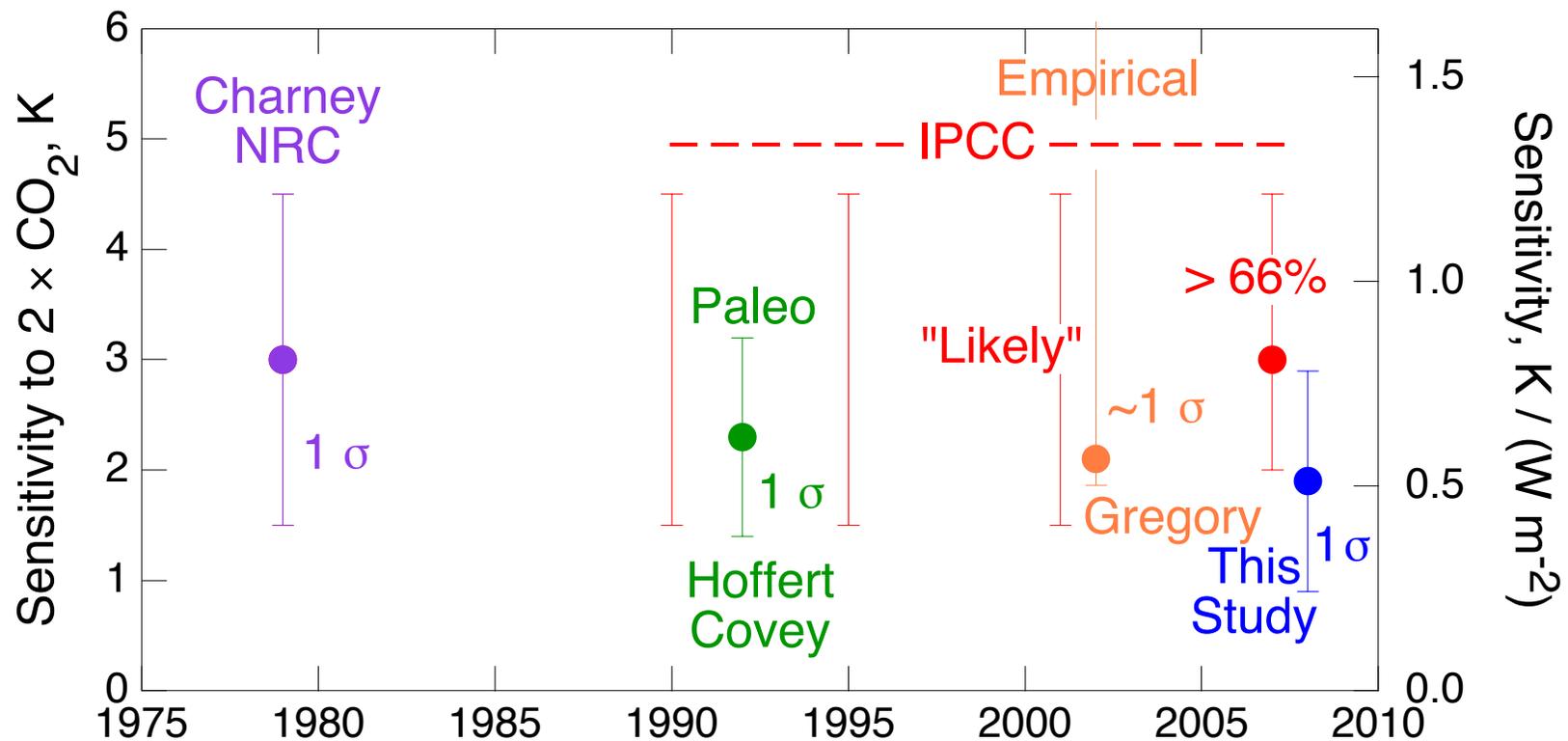
Climate system time constant is  $8.5 \pm 2.5$  years

# EVALUATION OF SENSITIVITY AND FORCINGS

Quantity	Unit	Value	1 $\sigma$
Effective global heat capacity $C$	W yr m <sup>-2</sup> K <sup>-1</sup>	<b>17</b>	<b>7</b>
Effective climate system time constant $\tau$	yr	<b>8.5</b>	<b>2.5</b>
Equilibrium climate sensitivity $S = \tau / C$	K/(W m <sup>-2</sup> )	<b>0.51</b>	<b>0.26</b>
Feedback factor $f$	–	<b>1.7</b>	
Equilibrium temperature increase for $2 \times \text{CO}_2$ , $\Delta T_{2\times}$	K	<b>1.9</b>	<b>1.0</b>
Total forcing over the 20 <sup>th</sup> century, $F_{20} = \Delta T_{20} / S$	W m <sup>-2</sup>	<b>1.1</b>	<b>0.6</b>
Forcing in 20 <sup>th</sup> century other than GHGs ( <i>mainly aerosols</i> ), $F_{20}^{\text{other}} = F_{20} - F_{20}^{\text{ghg}}$	W m <sup>-2</sup>	<b>-1.1</b>	<b>0.7</b>
Lag in temperature change, $\Delta T_{\text{lag}}$	K	<b>0.05</b>	

# CLIMATE SENSITIVITY ESTIMATES THROUGH THE AGES

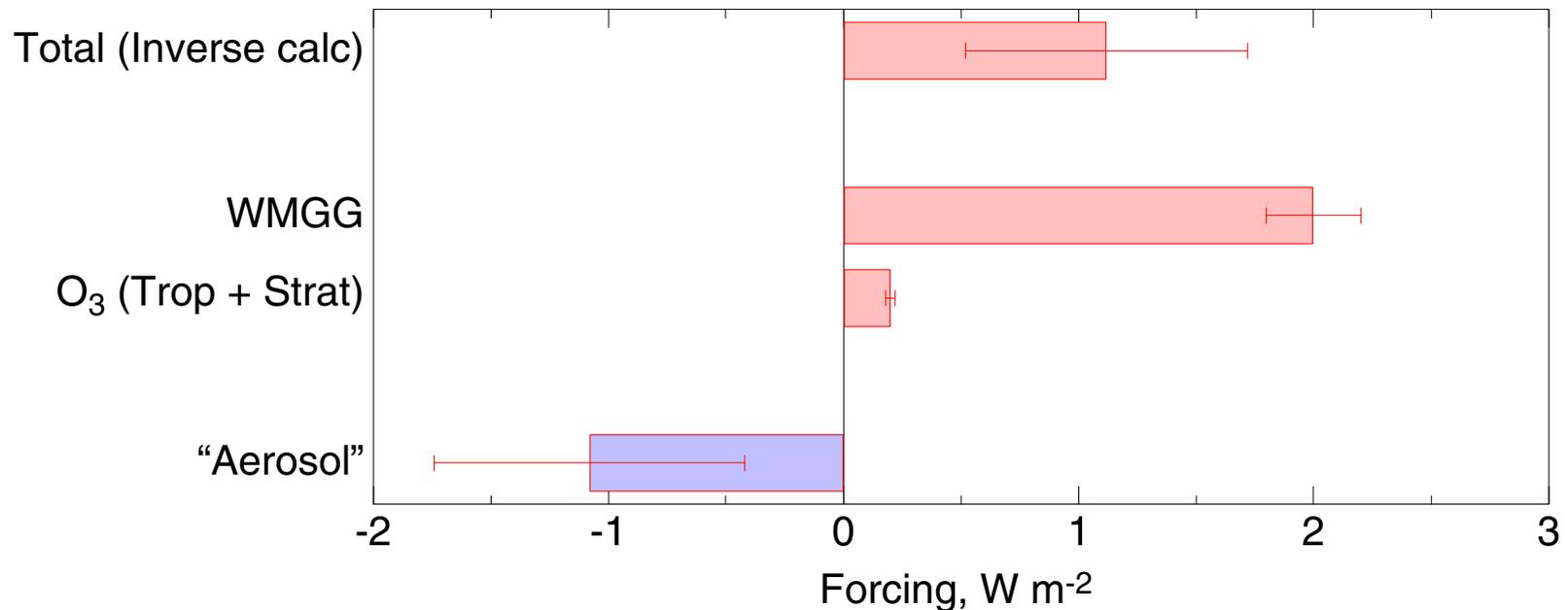
Estimates of central value and uncertainty range from specific approaches and major national and international assessments



*Sensitivity obtained in this study overlaps range from climate models, paleo, empirical; seems to rule out  $\Delta T_{2x} \gtrsim 3$  K.*

# INVERSE CALCULATION OF “AEROSOL” FORCING OVER TWENTIETH CENTURY

$$\text{“Aerosol” forcing} = \text{Total forcing} - \text{GHG forcing}$$



Total forcing remains uncertain to a factor of 3.

“Aerosol” forcing, calculated as residual, is presumably dominated by aerosols.

“Aerosol” forcing is substantial, with large uncertainty.

“Aerosol” forcing could be masking as much as 75% of GHG warming.

# CONCLUDING REMARKS

Traditional approaches to determination of Earth's climate sensitivity yield uncertainty of at least a factor of 3, largely because of uncertainty in aerosol forcing.

The energy balance approach offers a new independent determination of Earth's climate sensitivity that does not depend on knowledge of aerosol forcing.

This approach yields a sensitivity that is at the low end of current estimates and would seem to rule out high sensitivity.

The short time constant,  $\sim 8.5$  years, suggests little heating in the pipeline from time lags.

Aerosols could be masking up to 75% of GHG forcing and warming.

Nothing in the present study should be construed as diminishing the need for strenuous reduction in GHG emissions.

# FINAL REMARKS

This study is a first effort on this approach. I would hope that it would be refined by further research.

Would I bet the ranch on this analysis? Of course not.