

# EARTH'S HEAT UPTAKE COEFFICIENT AND TRANSIENT AND EQUILIBRIUM CLIMATE SENSITIVITIES

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*viewgraphs available at [www.ecd.bnl.gov/steve](http://www.ecd.bnl.gov/steve)*

# SOME SIMPLE QUESTIONS ABOUT CLIMATE CHANGE

How much has *Global Mean Surface Temperature* (GMST) increased over the industrial period?

What is the magnitude of *forcing* over the industrial period?

What is Earth's *climate sensitivity*?

What is the expected *equilibrium increase* in GMST?

Why hasn't GMST increased as much as expected?

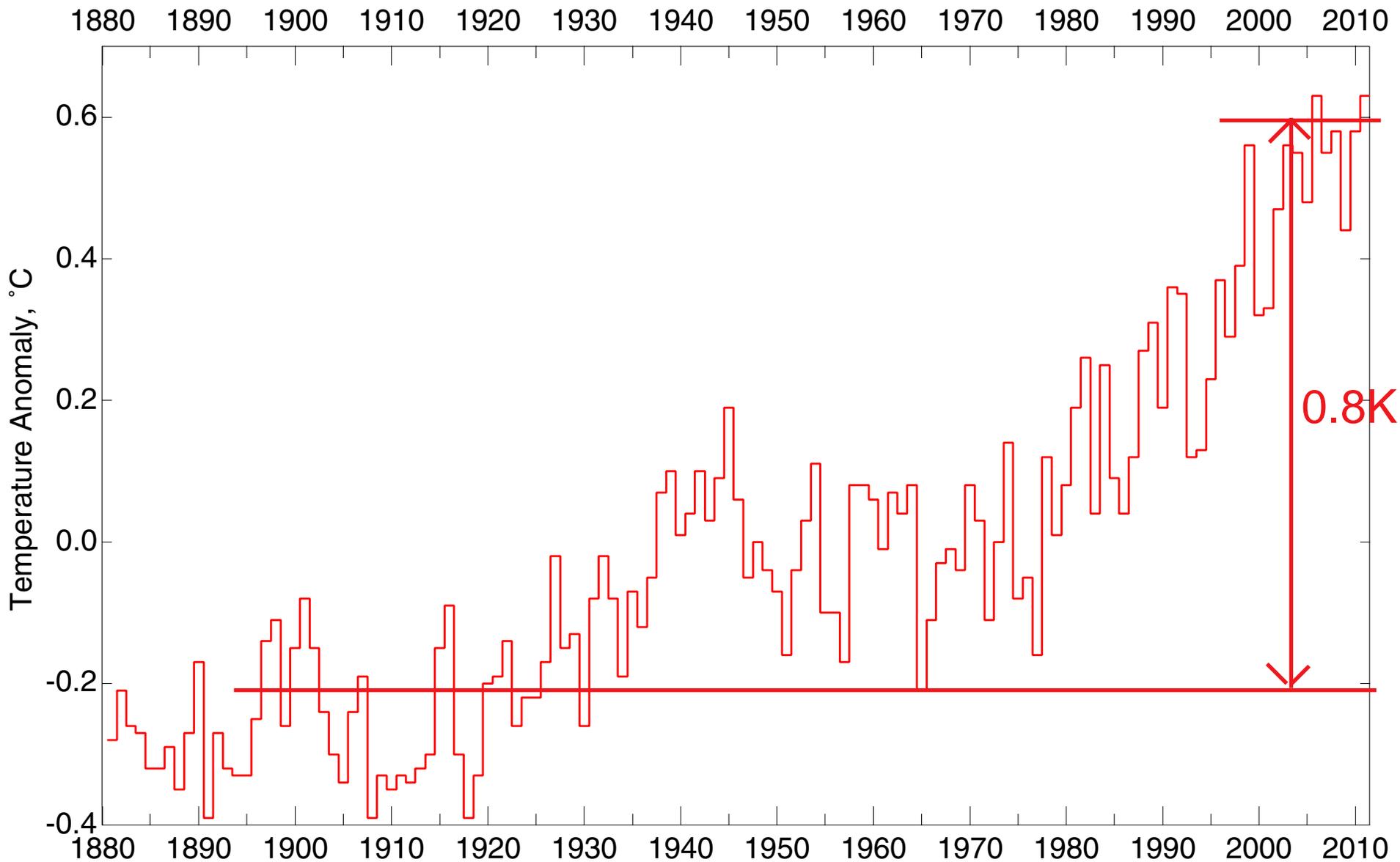
How much of this is due to *time lag of response* of the climate system? What are the *time constants* of the system?

How much is due to *offsetting forcing by tropospheric aerosols*?

What is the magnitude of the *planetary energy imbalance*?

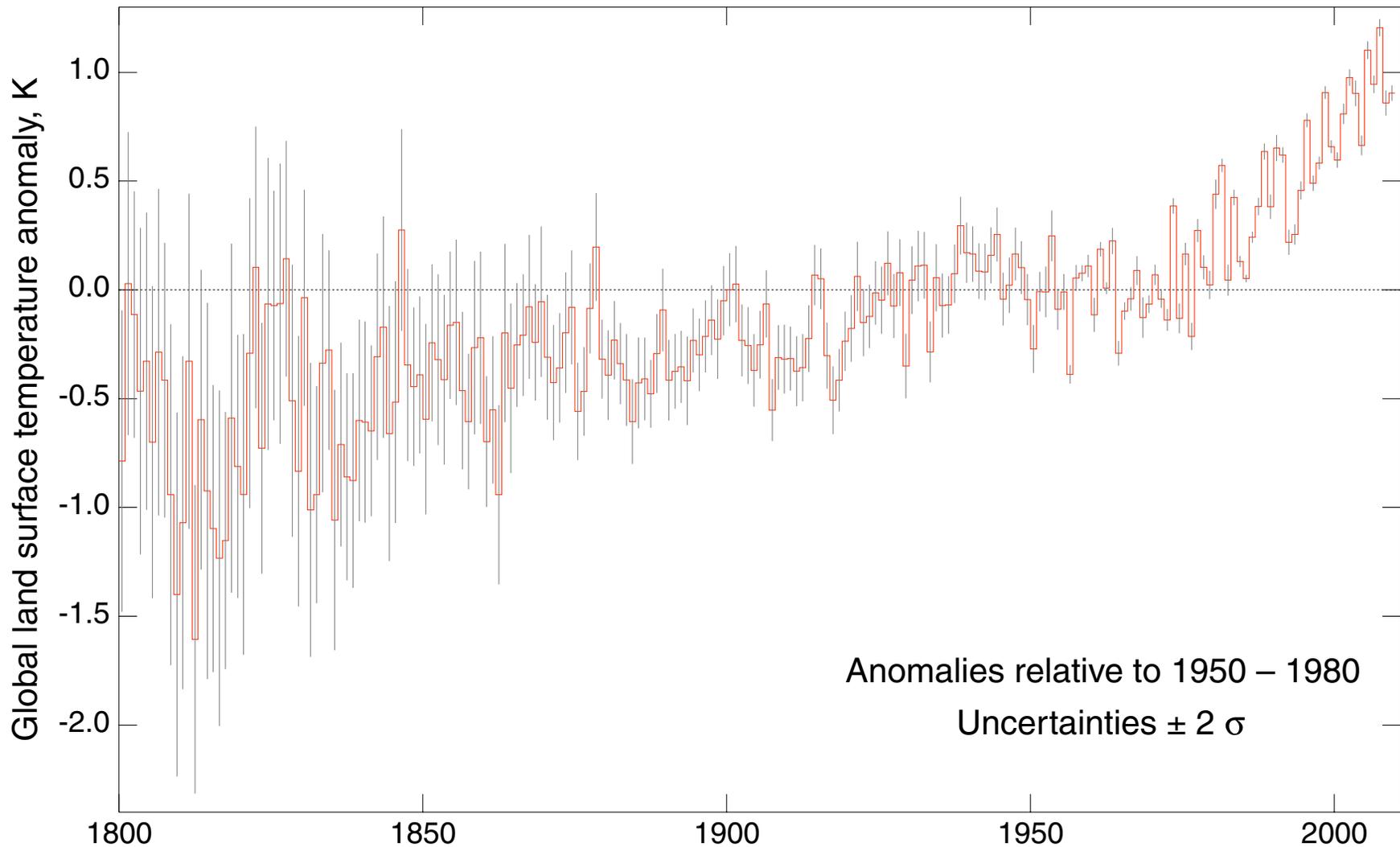
How much more warming is “*in the pipeline*” – committed warming?

# GLOBAL ANNUAL TEMPERATURE ANOMALY, 1880-2010



*Data: Goddard Institute for Space Studies*

# GLOBAL LAND SURFACE TEMPERATURE ANOMALY

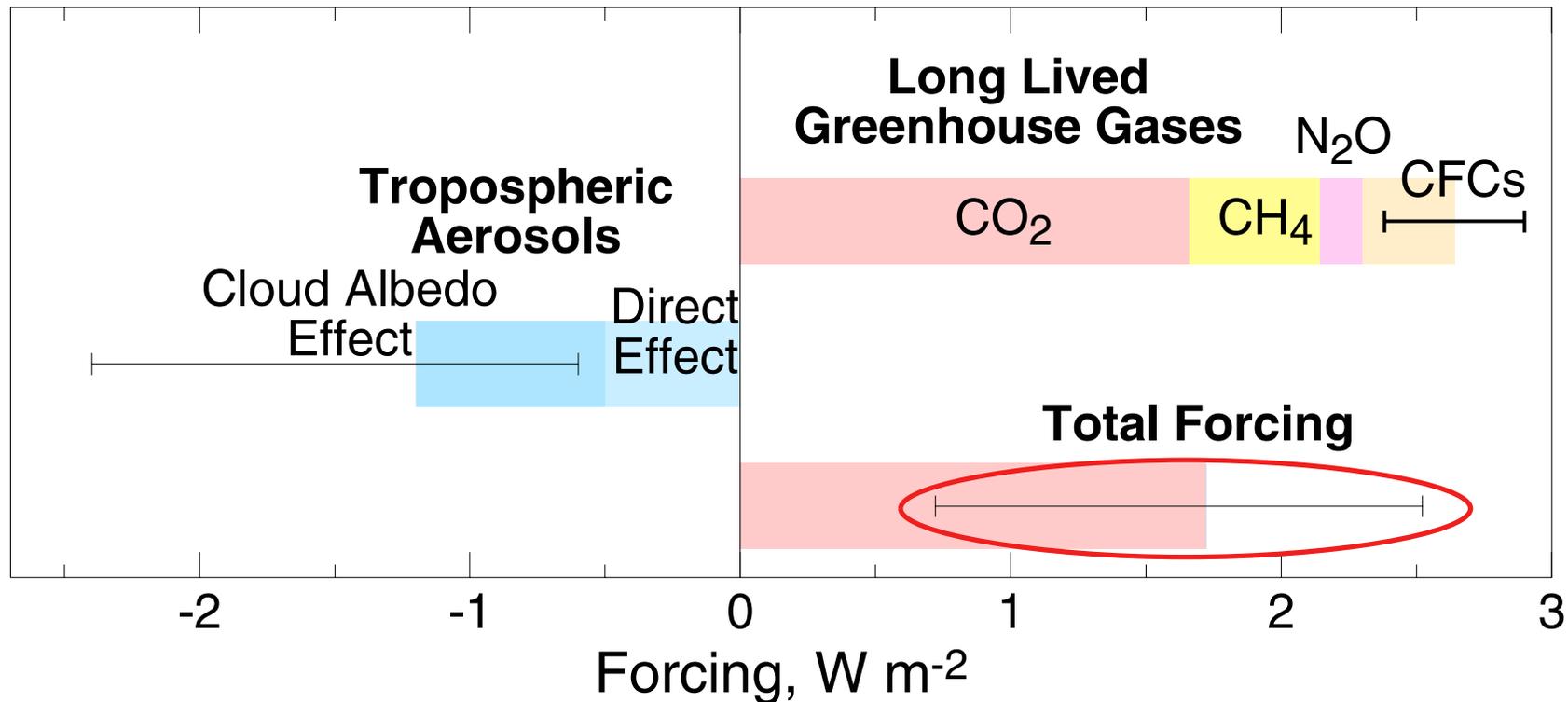


*Muller et al. (Berkeley Earth Project), submitted, 2011*

Independent analysis confirms increase in temperature over 20<sup>th</sup> century.

# CLIMATE FORCINGS OVER THE INDUSTRIAL PERIOD

Extracted from IPCC AR4 (2007)



Aerosol forcing may offset much of the greenhouse gas forcing.

*Uncertainty in total forcing is dominated by uncertainty in aerosol forcing.*

# EQUILIBRIUM CLIMATE SENSITIVITY

Equilibrium change  
in global mean  
surface temperature = Climate  
sensitivity  $\times$  Forcing

$$\Delta T = S_{\text{eq}} \times F$$

$S$  is *equilibrium* sensitivity. Units:  $\text{K}/(\text{W m}^{-2})$

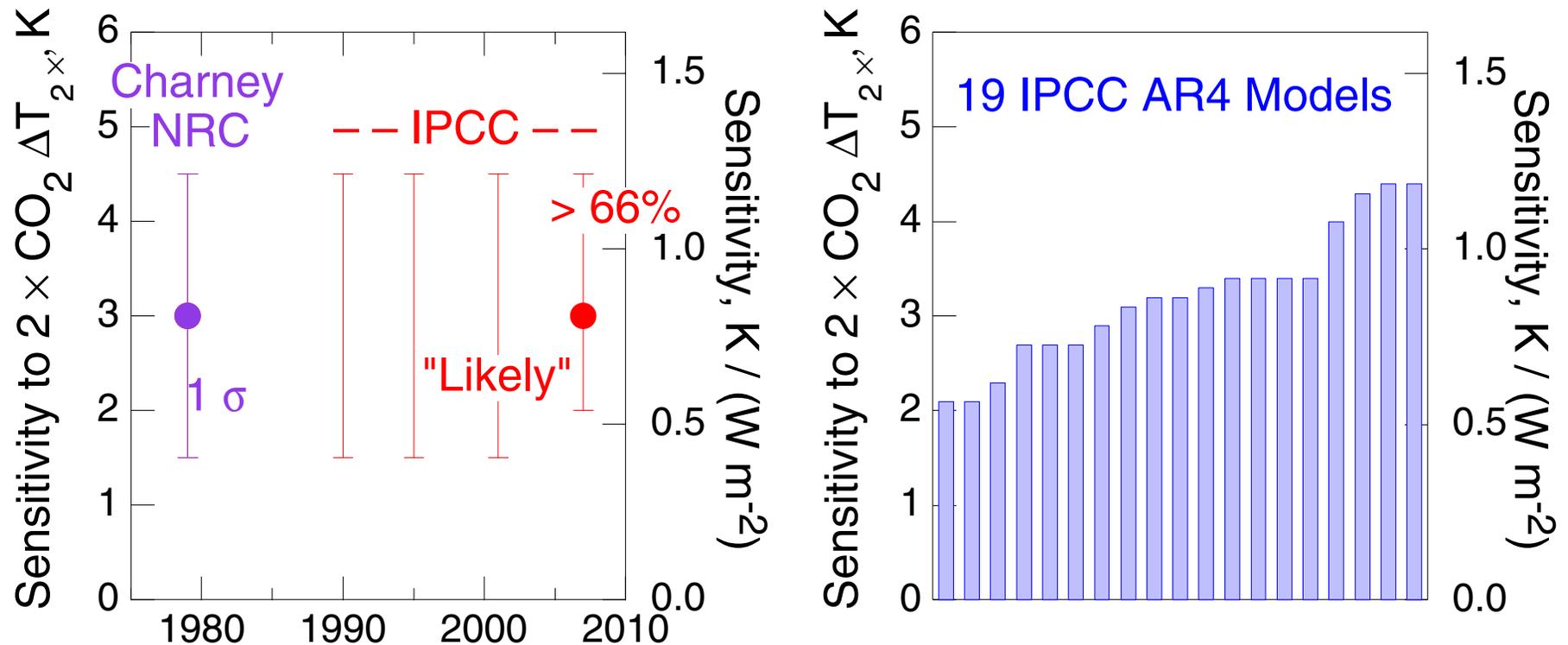
Sensitivity is commonly expressed as “CO<sub>2</sub> doubling temperature”

$$\Delta T_{2\times,\text{eq}} \equiv S_{\text{eq}} \times F_{2\times}$$

where  $F_{2\times}$  is the CO<sub>2</sub> doubling forcing, *ca.*  $3.7 \text{ W m}^{-2}$ .

# ESTIMATES OF EARTH'S CLIMATE SENSITIVITY AND ASSOCIATED UNCERTAINTY

Major national and international assessments and current climate models



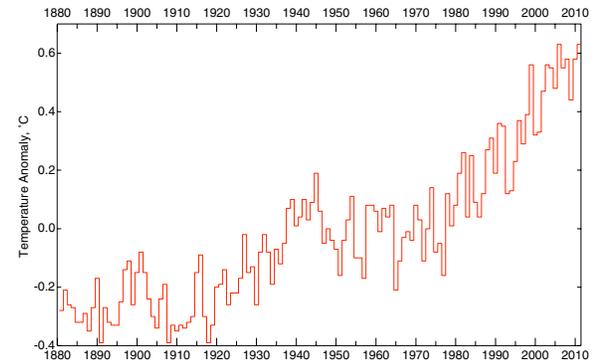
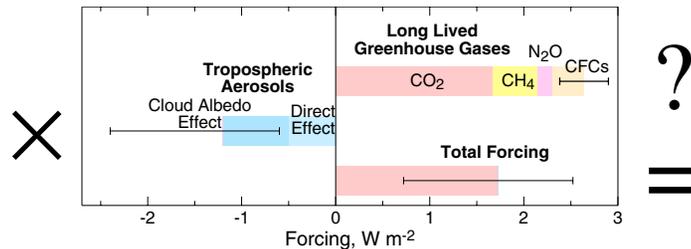
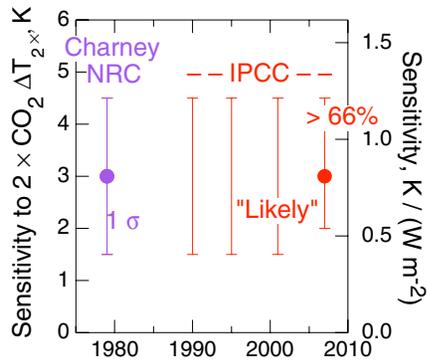
Current estimates of Earth's climate sensitivity are centered about a CO<sub>2</sub> doubling temperature  $\Delta T_{2\times} = 3$  K, but with substantial uncertainty.

Range of sensitivities of current models roughly coincides with IPCC “likely” range.

# EQUILIBRIUM TEMPERATURE CHANGE

Climate sensitivity  $\times$  Forcing = Equilibrium change in global mean surface temperature

$$S \times F \stackrel{?}{=} \Delta T$$

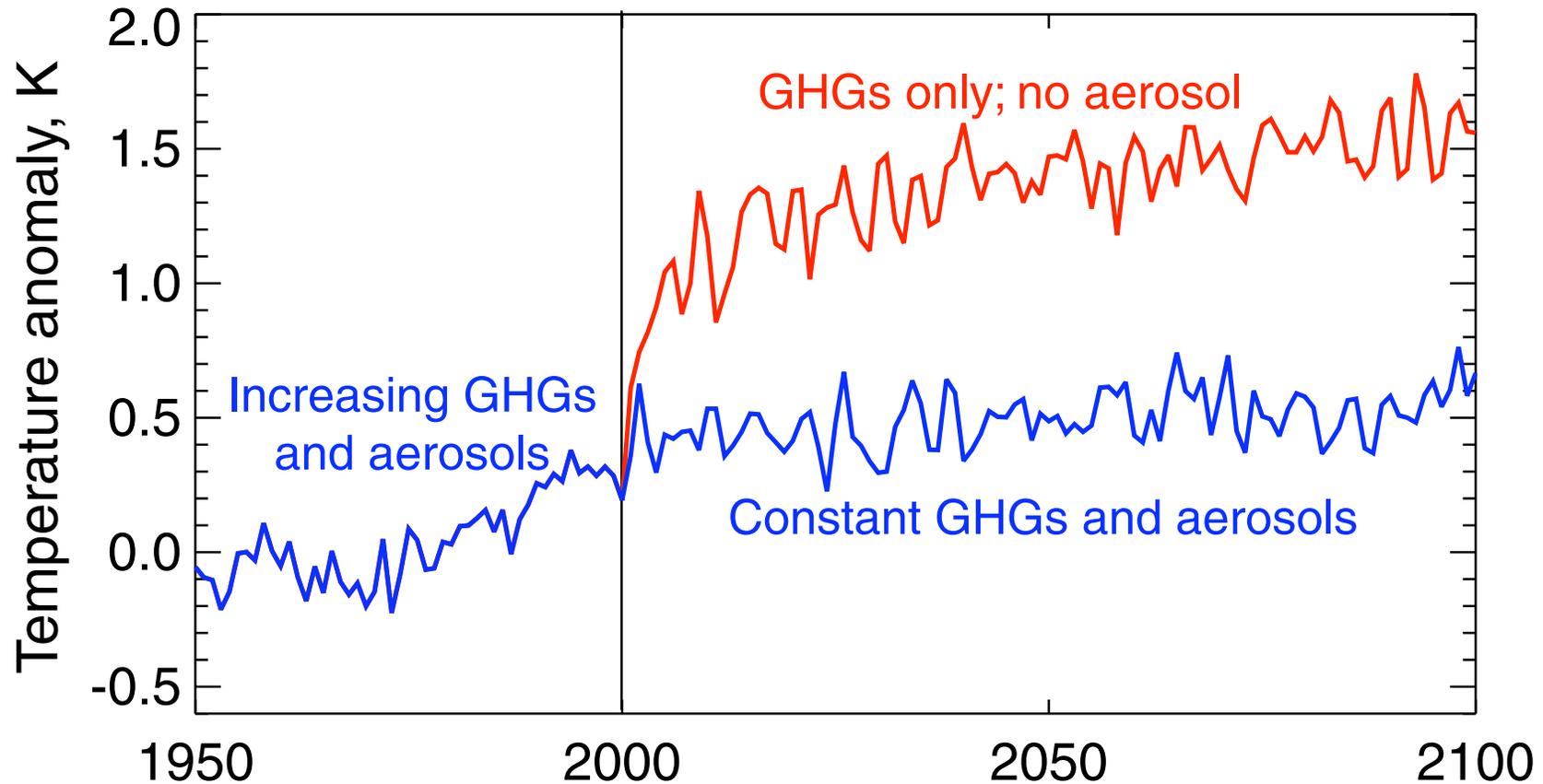


$$\begin{array}{l}
 0.54 \\
 0.81 \\
 1.21
 \end{array}
 \text{ K}/(\text{W m}^{-2}) \times \begin{array}{l} 1.1 \\ 1.6 \\ 2.0 \end{array} \text{ W m}^{-2} = \begin{array}{l} 0.7 \\ 1.3 \\ 2.0 \end{array} \text{ K}$$

( $\sim 1\sigma$ )

# GLOBAL TEMPERATURE RESPONSE TO TURNING OFF AEROSOL EMISSIONS

Experiment with ECHAM-5 GCM

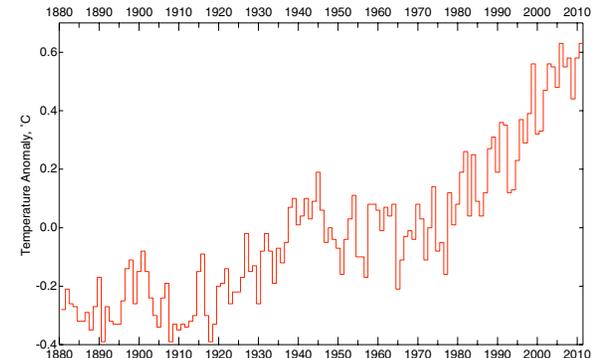
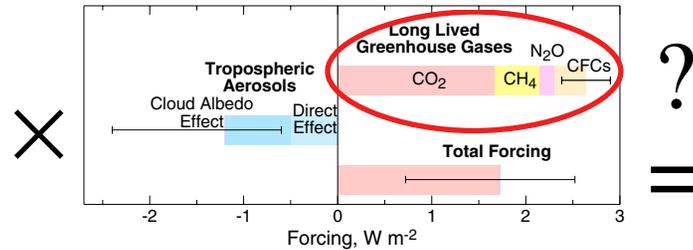
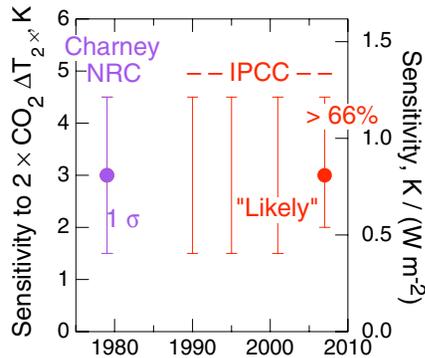


*Modified from Brasseur and Roeckner, GRL, 2005*

For constant GHGs and aerosols, temperature remains near year 2000 value. Without aerosol offset to GHG forcing temperature rapidly increases. However the magnitude of the aerosol offset is unknown.

# For forcing by long-lived greenhouse gases only

$$\Delta T_{\text{LLGHG}} = S \times F_{\text{LLGHG}}$$

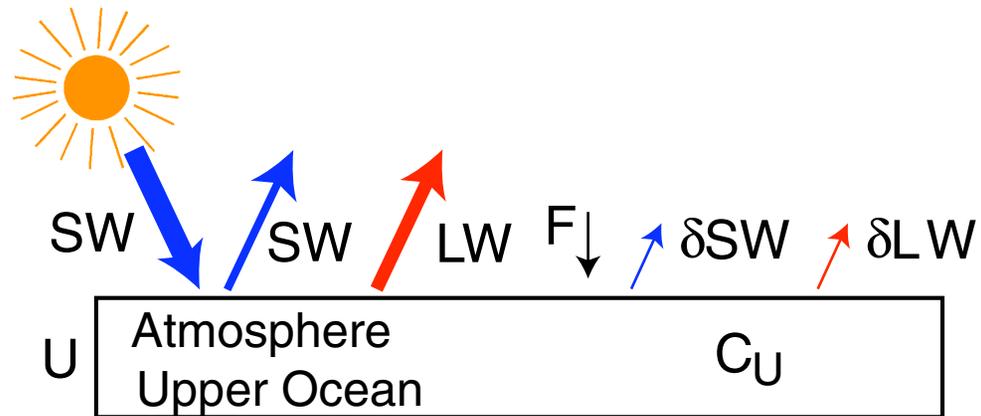


$$\begin{array}{l} 0.54 \\ 0.81 \\ 1.21 \end{array} \text{ K}/(\text{W m}^{-2}) \times \begin{array}{l} 2.47 \\ 2.60 \\ 2.73 \end{array} \text{ W m}^{-2} = \begin{array}{l} 1.4 \\ 2.1 \\ 3.2 \end{array} \text{ K}$$

Improved knowledge of forcings and climate sensitivity is essential for informed policymaking.

**OBSERVATIONALLY BASED  
DETERMINATION  
OF CLIMATE SENSITIVITY VIA  
ENERGY BALANCE MODELS**

# *Single compartment climate model*



***Energy conservation in the climate system:***

$$\frac{dH}{dt} \equiv N = Q - E$$

$H$  = planetary heat content;

$N$  = net heating rate of planet;

$Q$  = absorbed shortwave at TOA;

$E$  = emitted longwave at TOA.

***Unperturbed steady state (equilibrium) climate:***

$$N = 0; \quad Q_0 = E_0$$

*Net heating rate with external forcing  $F$  applied:*

$$N(t) = Q(t) - E(t) + F(t)$$

*Initially after onset of forcing*

$$Q = Q_0; \quad E = E_0; \quad N = F$$

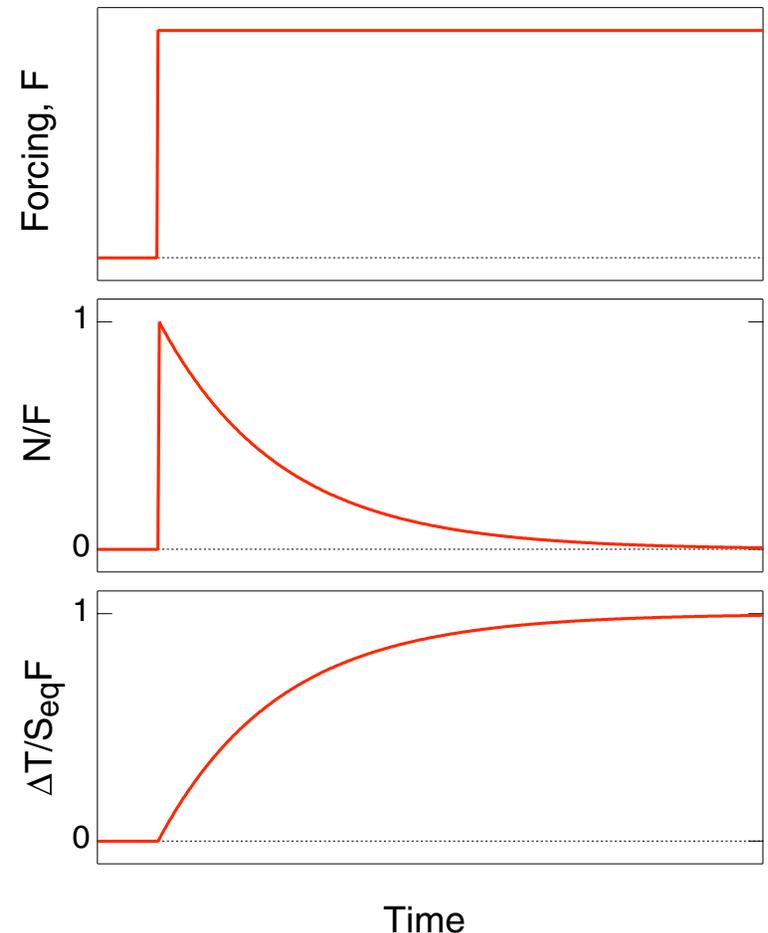
*Climate response to forcing*

$$N(t) = F(t) + \frac{\partial(Q - E)}{\partial T} \Delta T(t)$$

$$N(t) = F(t) - \lambda \Delta T(t)$$

where  $\lambda \equiv -\frac{\partial(Q - E)}{\partial T}$  is *climate response coefficient*.

$\lambda$  is a geophysical property of Earth's climate system.



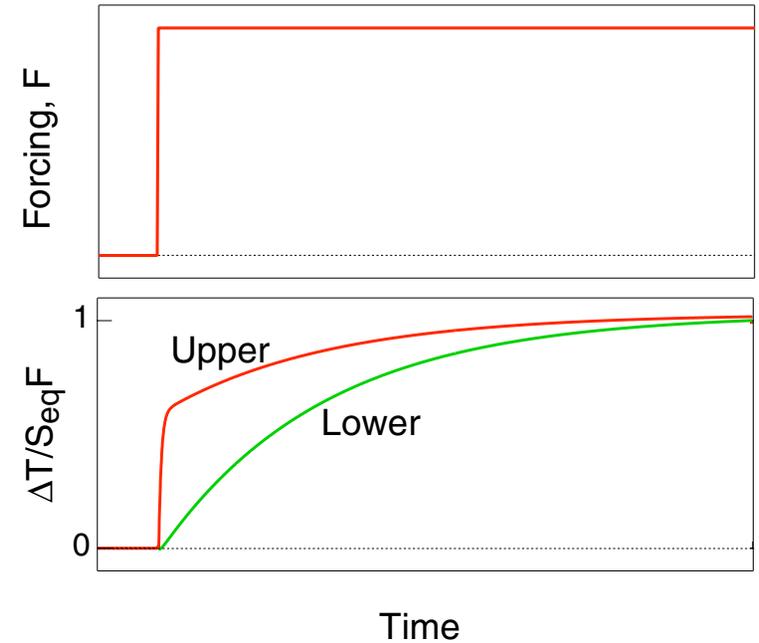
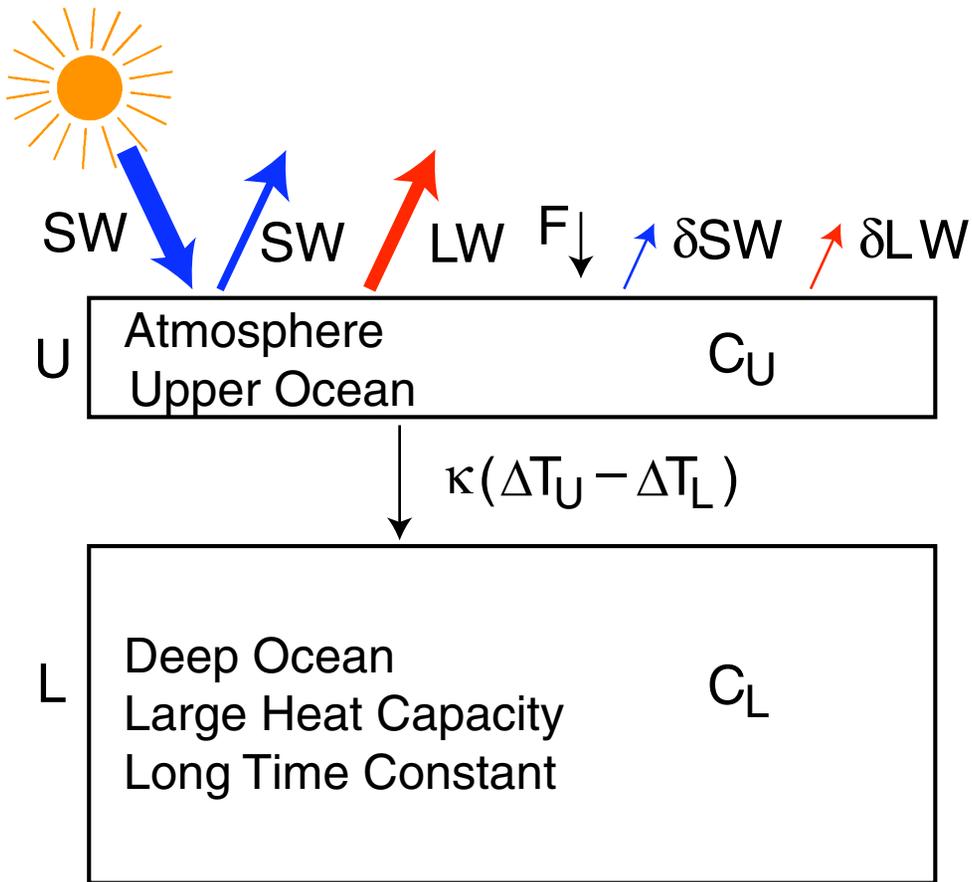
*At new steady state (equilibrium) following application of constant forcing  $F$*

$$N = 0; \quad \lambda \Delta T = F; \quad \Delta T = \lambda^{-1} F = S_{\text{eq}} F$$

$S_{\text{eq}}$  = *equilibrium climate sensitivity* =  $\lambda^{-1}$ .

$S_{\text{eq}}$  is a geophysical property of Earth's climate system.

# Two compartment climate model



# PREDECESSORS TO THIS MODEL

Gregory,  
*Climate Dynamics*,  
2001

$$cd_u \frac{dT_u}{dt} = H - k(T_u - T_1)$$

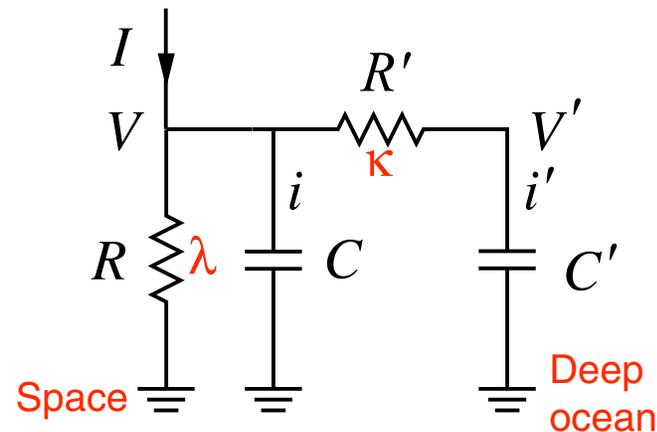
$$cd_1 \frac{dT_1}{dt} = k(T_u - T_1)$$

Held et al,  
*J. Climate*, 2010

$$c_F \frac{dT}{dt} = \mathcal{F} - \beta T - \gamma(T - T_D)$$

$$c_D \frac{dT_D}{dt} = \gamma(T - T_D)$$

Schwartz,  
*JGR*, 2008



# EMPIRICAL DETERMINATION OF COMPARTMENT HEAT CAPACITIES

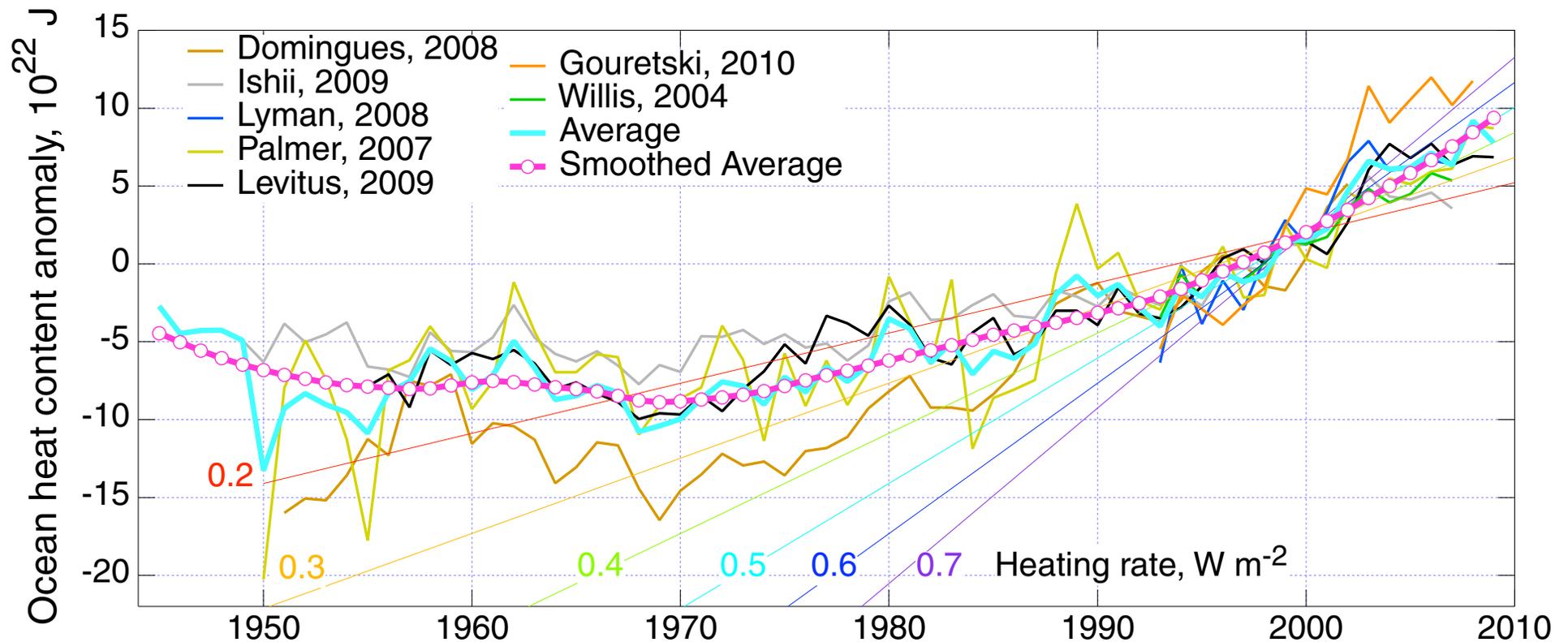
*Hypothesis: Planetary heat content increases linearly with surface temperature  $\Delta T$ .*

*Plot  $H(t)$  vs  $\Delta T(t)$ ; determine  $C_U$  as slope.*

Calculate  $C_L$  from volume of world ocean.

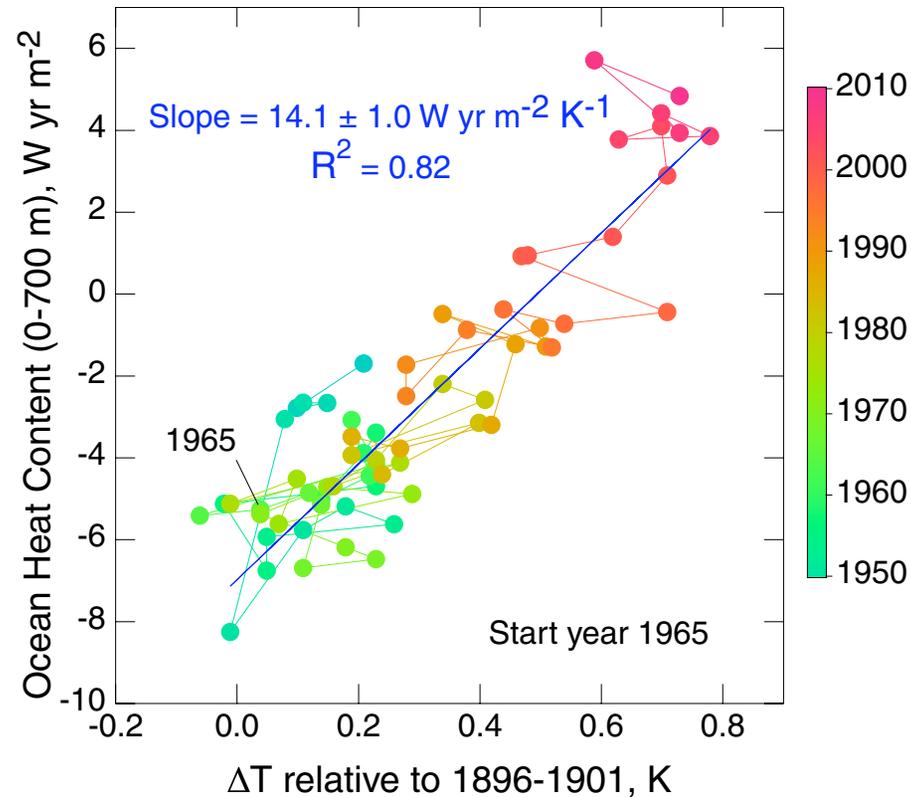
$C_U$  and  $C_L$  are geophysical properties of Earth's climate system.

# Heat content of global ocean



Heat content is from XBT soundings, later Argo robotic buoys.  
Uncertainties from representativeness, techniques ...  
Smoothed curve is LOWESS fit.  
Monotonic increase since about 1970.

# *World ocean heat content vs temperature anomaly*

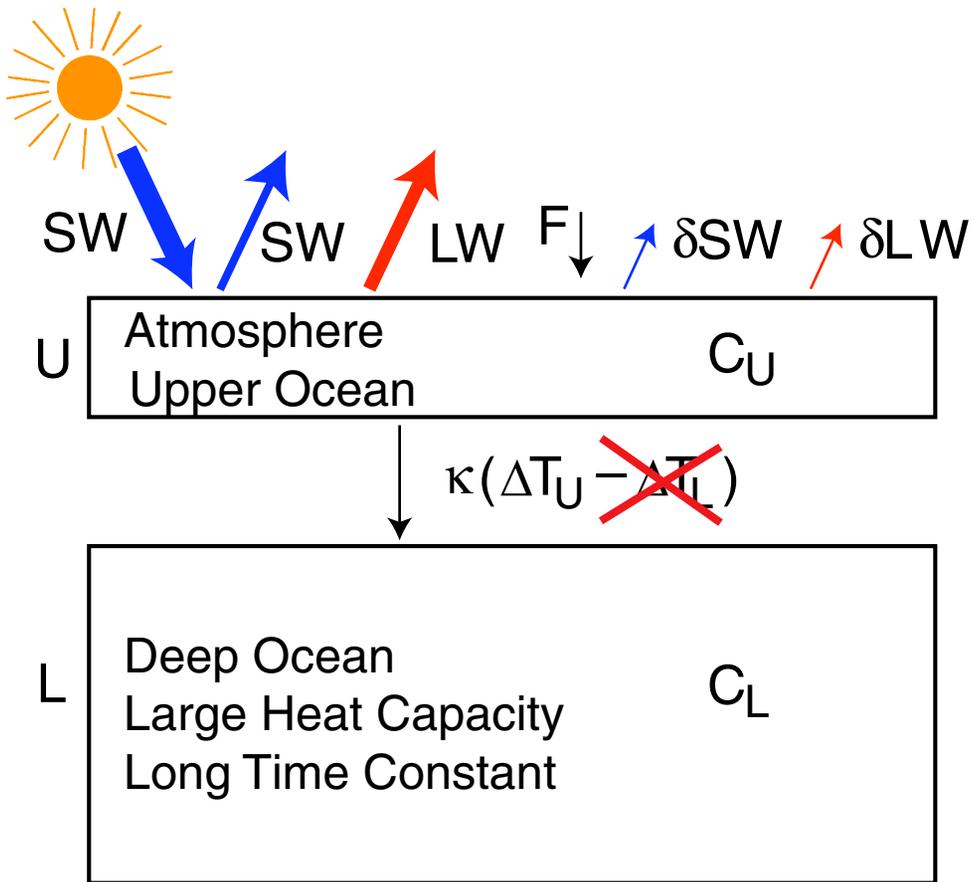


*Heat content varies linearly with temperature anomaly.*

Heat capacity determined as slope, accounting for additional heat sinks (deep ocean, air, land, ice melting).

Upper compartment heat capacity  $C_U = 21.8 \pm 2.1\ W\ yr\ m^{-2}\ K^{-1}$  ( $1\ \sigma$ , based on fit, not systematic errors); equivalent to 170 m of seawater, globally.

# *Two compartment climate model*



# EMPIRICAL DETERMINATION OF HEAT EXCHANGE COEFFICIENT

*Hypothesis: Planetary heating rate proportional to  $\Delta T$*

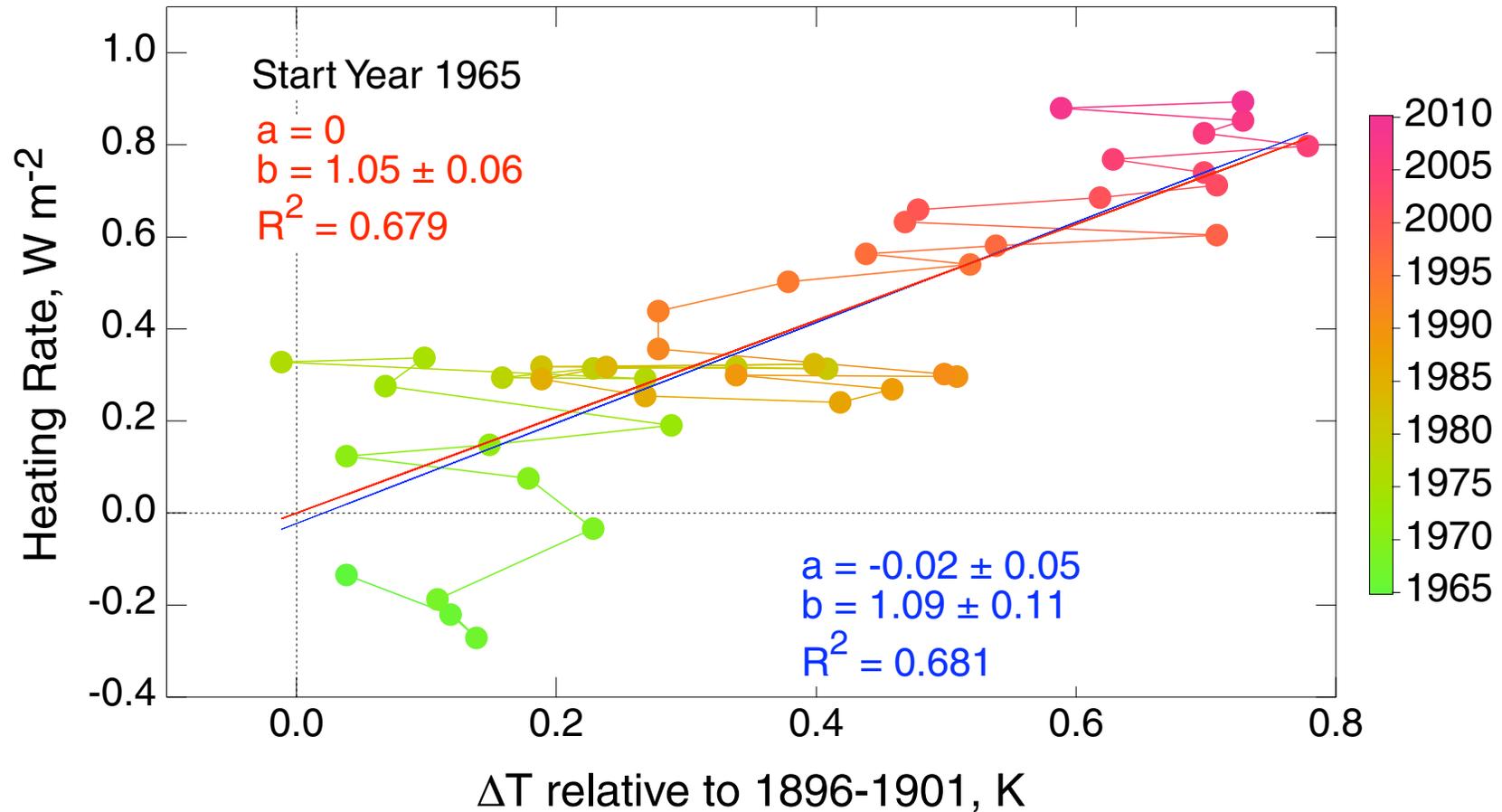
$$N(t) = \kappa \Delta T(t)$$

$\kappa =$  *heat exchange coefficient.*

**Plot**  $N(t)$  vs  $\Delta T(t)$ ; determine  $\kappa$  as slope (with zero origin).

$\kappa$  is a geophysical property of Earth's climate system.

# *Global heating rate vs temperature anomaly*



Heating rate (time derivative of ocean heat content) is *linearly proportional* to temperature anomaly.

Heat exchange coefficient  $\kappa = 1.05 \pm 0.06 \text{ W m}^{-2} \text{ K}^{-1}$   
( $1\sigma$ , based on fit, not systematic errors).

# TRANSIENT CLIMATE SENSITIVITY

*Assumption: Planetary heating rate proportional to  $\Delta T$*

$$N(t) = \kappa \Delta T(t)$$

$\kappa =$  *heat exchange coefficient*, a geophysical property of Earth's climate system.

$$N(t) = F(t) - \lambda \Delta T(t)$$

$$F(t) = (\kappa + \lambda) \Delta T(t); \quad \Delta T(t) = (\kappa + \lambda)^{-1} F(t) = S_{\text{tr}} F(t)$$

$S_{\text{tr}} =$  *transient climate sensitivity*,  $S_{\text{tr}} \equiv (\kappa + \lambda)^{-1}$ ,  
a geophysical property of Earth's climate system

Contrast equilibrium sensitivity,  $S_{\text{eq}} = \lambda^{-1}$

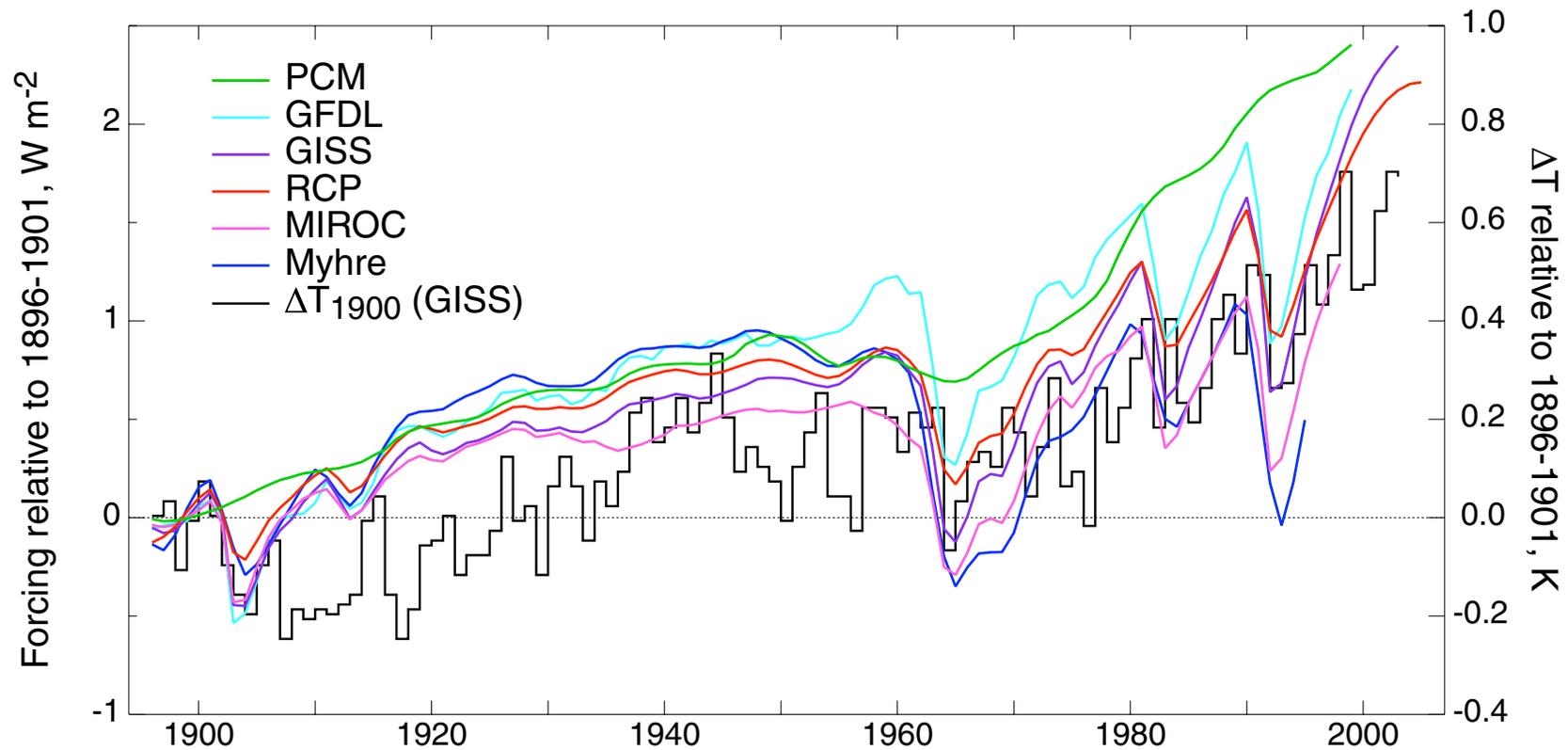
# FORCING DATA SETS EXAMINED IN THIS STUDY

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Forcing Data Set	Forcing, 1900-1990, W m <sup>-2</sup>
PCM, Parallel Climate Model, National Center for Atmospheric Research; Meehl et al., 2003	2.1
GFDL, Geophysical Fluid Dynamics Laboratory; Held et al., 2010	1.9
GISS, Goddard Institute for Space Studies; Hansen et al., 2005	1.6
RCP - Representative Concentration Pathways; Meinshausen et al., 2010	1.6
MIROC, Model for Interdisciplinary Research On Climate; Takemura et al., 2006	1.1
Myhre et al., 2001	1.0

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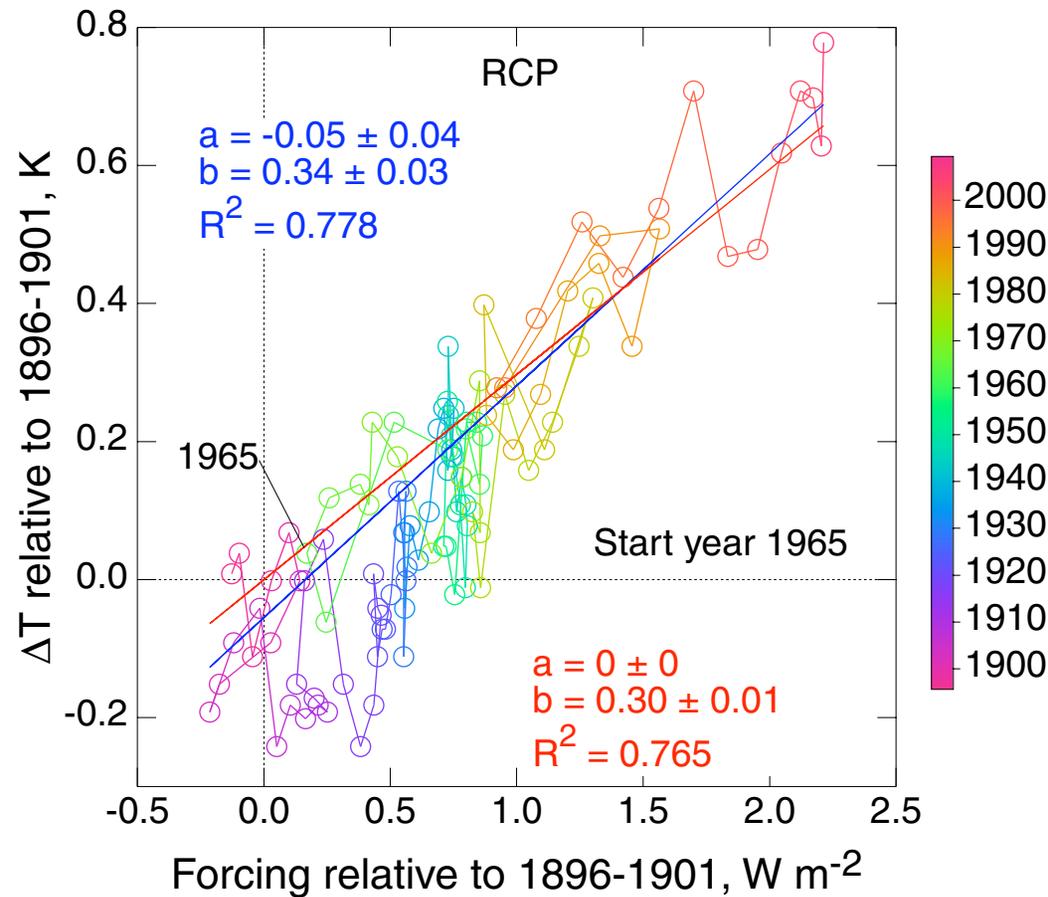
# *Forcings and temperature anomaly over the twentieth century*



Forcings from published studies (convolved with 3-year exponential to smooth out fast fluctuations) are input to the determination of sensitivities.

Forcings and temperature anomaly are more or less coherent.

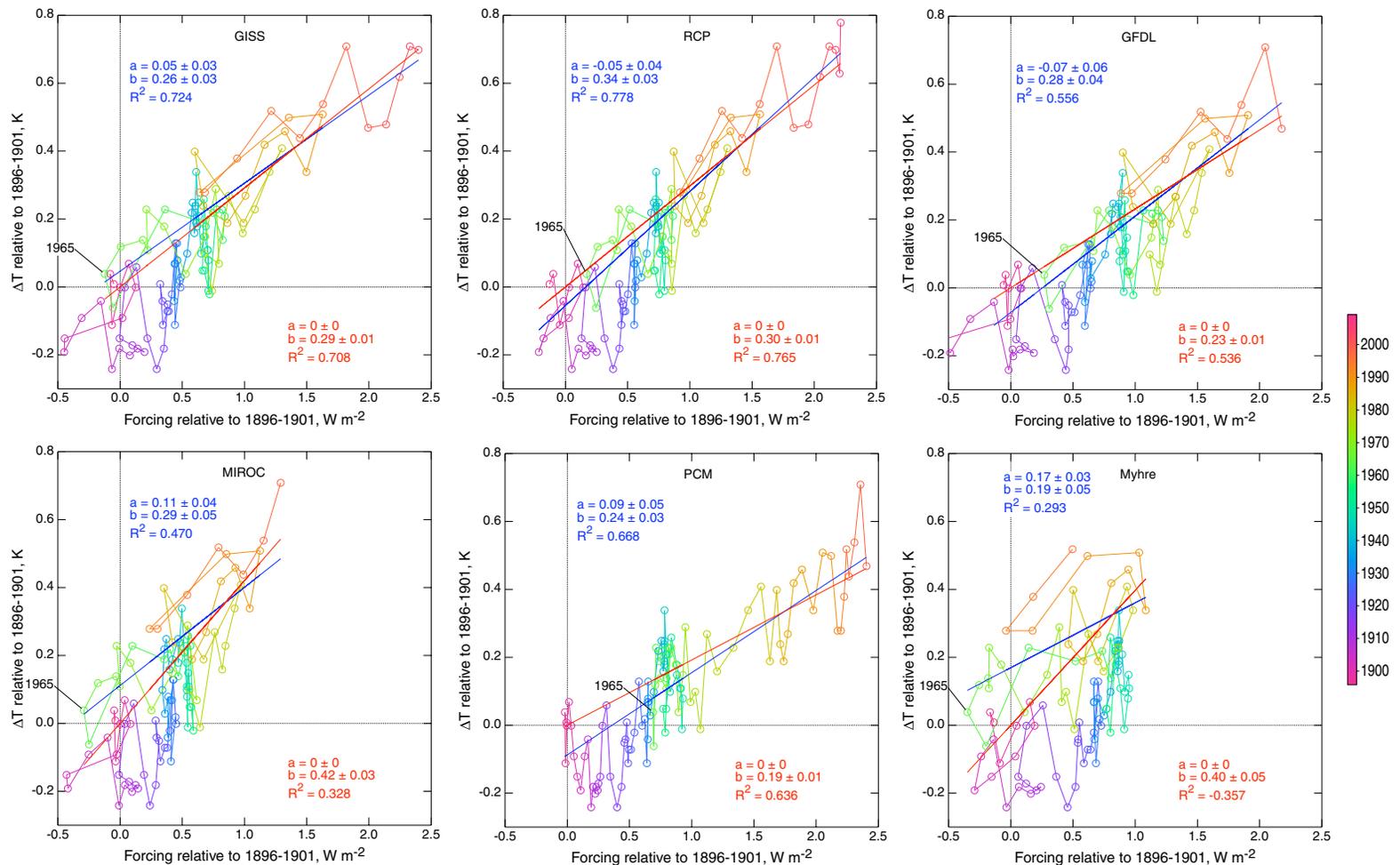
# Temperature anomaly vs forcing – RCP forcing dataset



RCP: “Representative Concentration Pathways” – default for IPCC AR5 climate model runs.

$\Delta T$  is linearly proportional to forcing, consistent with transient sensitivity model; slope yields *transient* sensitivity.

# Temperature anomaly vs forcing – 6 forcing datasets



$\Delta T$  is *linearly proportional* to forcing for most forcing datasets, consistent with model.

Slope yields *transient* sensitivity.

Transient sensitivity differs for different forcing datasets.

# SUMMARY OF FINDINGS

**GEOPHYSICAL QUANTITIES  
DETERMINED IN THIS STUDY**  
(Independent of Forcing)

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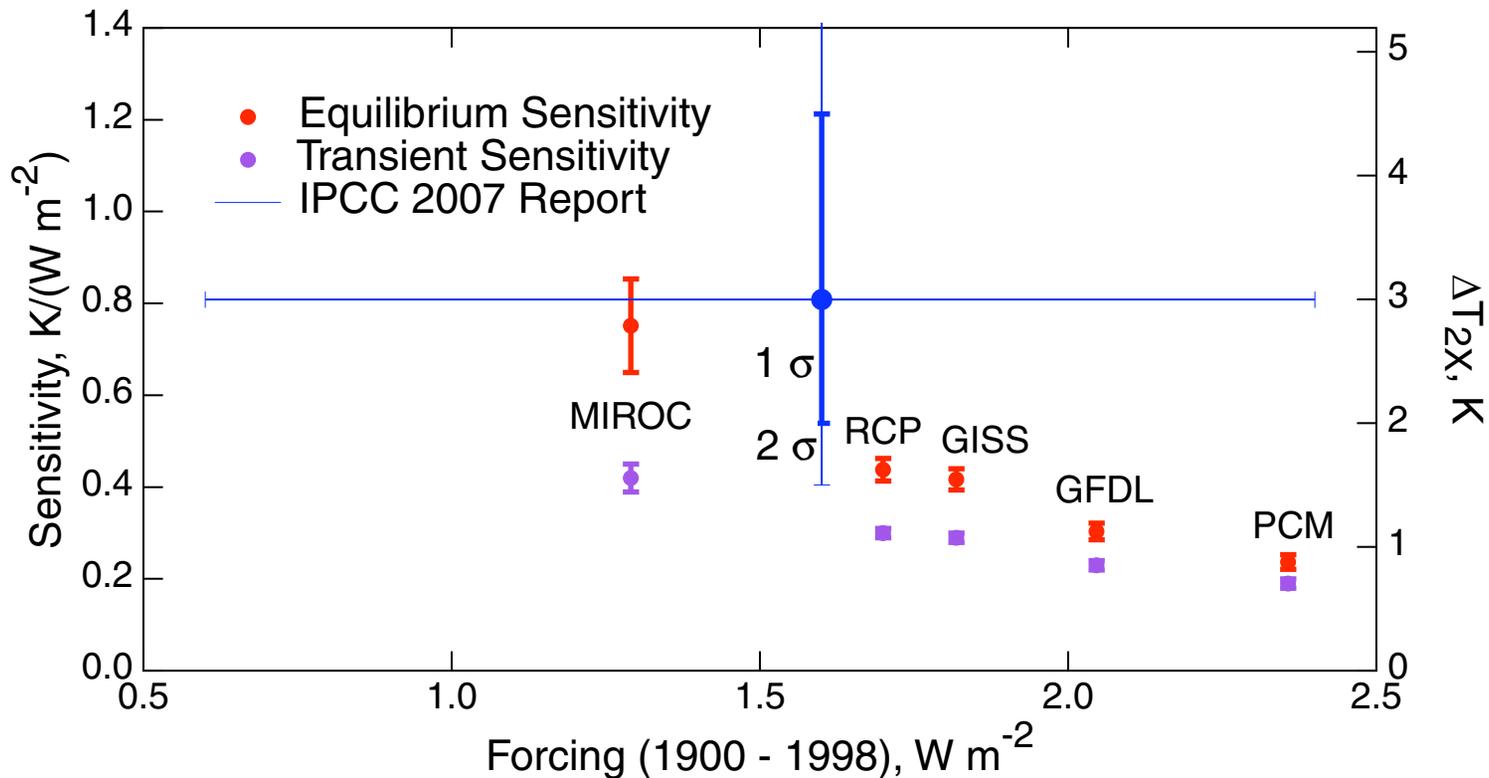
Quantity	Unit	Value	$\sigma$
$\kappa$	W m <sup>-2</sup> K <sup>-1</sup>	1.05	0.06
$C_U$	W yr m <sup>-2</sup> K <sup>-1</sup>	21.8	2.1
$C_L$	W yr m <sup>-2</sup> K <sup>-1</sup>	340	

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# FORCING-DEPENDENT QUANTITIES DETERMINED IN THIS STUDY

Quantity	Unit	Forcing Data Set				
		PCM	GFDL	GISS	RCP	MIROC
$F(1900-1990)$	$\text{W m}^{-2}$	2.1	1.9	1.6	1.6	1.1
$S_{\text{tr}}$	$\text{K (W m}^{-2})^{-1}$	0.19	0.23	0.29	0.30	0.42
$\Delta T_{2\times, \text{tr}}$	K	0.70	0.85	1.08	1.11	1.56
$S_{\text{eq}}$	$\text{K (W m}^{-2})^{-1}$	0.24	0.30	0.42	0.44	0.75
$\Delta T_{2\times, \text{eq}}$	K	0.88	1.12	1.54	1.62	2.78
$\tau_s$	yr	4.1	5.0	6.3	6.5	9.2
$\tau_l$	yr	405	427	466	473	579

# *Climate sensitivities vs forcing*



*Equilibrium sensitivities are **lower to much lower** than IPCC central estimate. **Transient sensitivities are even lower.***

*Inferred transient and equilibrium sensitivities vary inversely with assumed twentieth century forcing.*

*Determination of sensitivities remains hostage to uncertainty in forcing, due mainly to aerosols.*

## *Response times in two-compartment model*

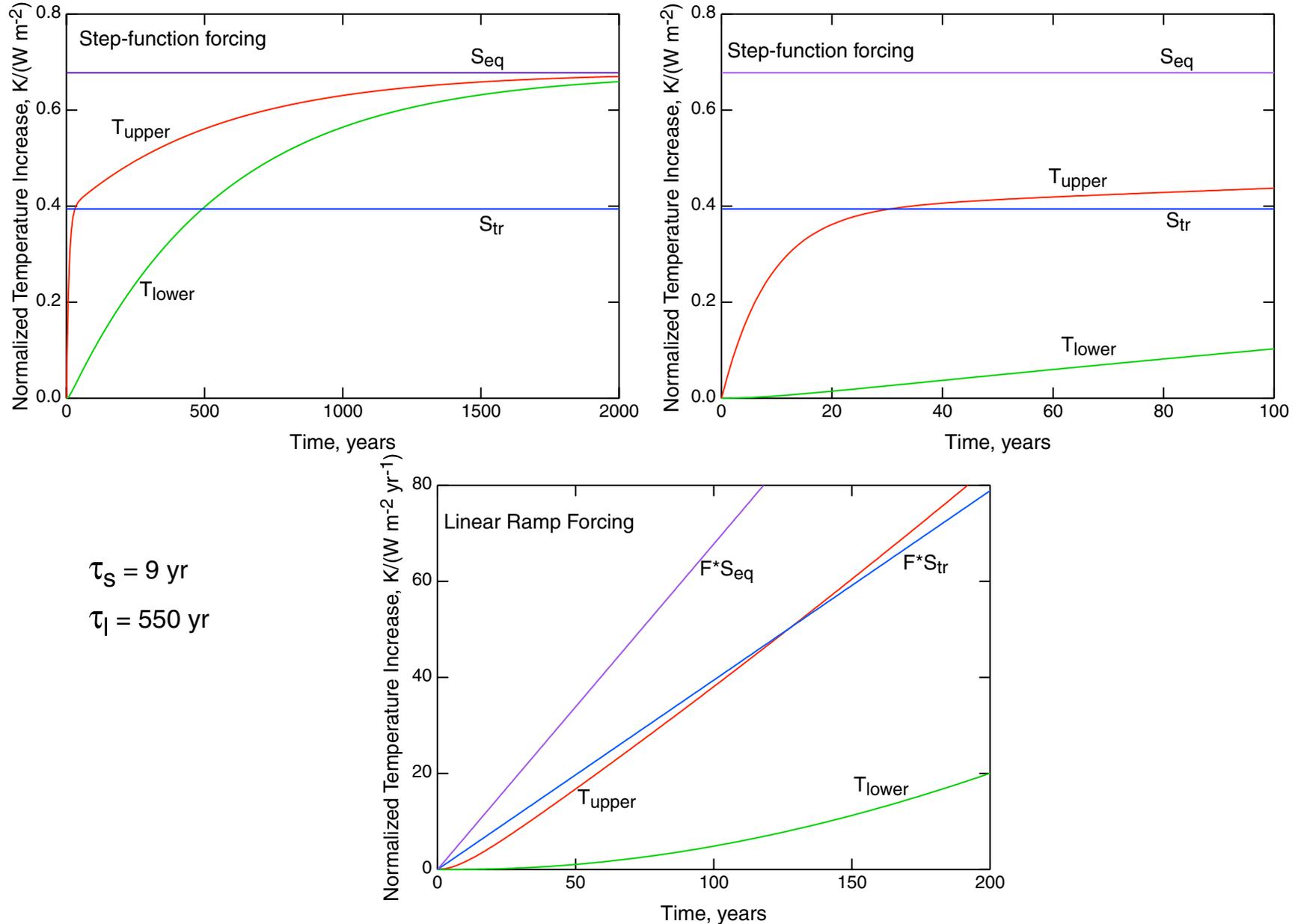
$$\tau_s = \frac{C_U}{\kappa + \lambda} \quad \tau_1 = C_L \left( \frac{1}{\lambda} + \frac{1}{\kappa} \right)$$

Obtained from eigenvalues, to first order in  $C_U / C_L$ .

Time constants can be evaluated from heat capacities and equilibrium and transient sensitivities.

$\tau_s$  and  $\tau_1$  are geophysical properties of Earth's climate system.

# Temperature response to forcings in 2-compartment system



Transient sensitivity yields good estimate over initial 100-200 years.

# PREDECESSORS TO THIS STUDY

Gregory,  
*Climate Dynamics*,  
2001

$$cd_u \frac{dT_u}{dt} = H - k(T_u - T_1)$$

$$\kappa = 1.6 \text{ (W m}^{-2}\text{) / K}$$

$$\tau_s = 12 \text{ yr}$$

$$cd_1 \frac{dT_1}{dt} = k(T_u - T_1)$$

Held et al,  
*J. Climate*, 2010

$$c_F \frac{dT}{dt} = \mathcal{F} - \beta T - \gamma(T - T_D)$$

$$\kappa = 1.3 \text{ (W m}^{-2}\text{) / K}$$

$$\Delta T_{2\times,eq} = 3.4 \text{ K}$$

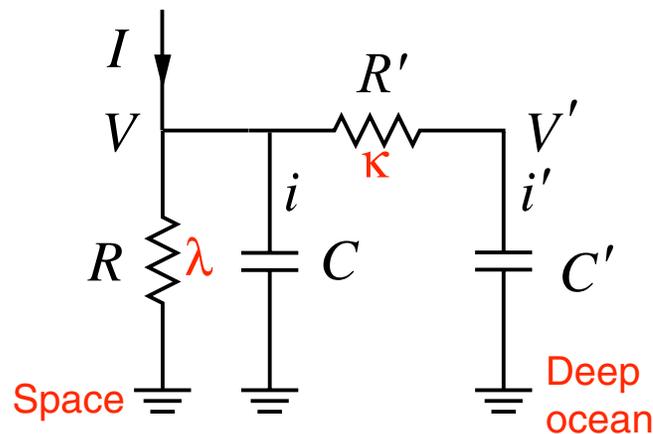
$$\Delta T_{2\times,tr} = 1.5 \text{ K}$$

$$c_D \frac{dT_D}{dt} = \gamma(T - T_D)$$

$$\tau_s = 4 \text{ yr}$$

$$\tau_1 = \text{“recalcitrant”}$$

This study



$$\kappa = 1.1 \text{ (W m}^{-2}\text{) / K}$$

$$\Delta T_{2\times,tr} = 0.7 - 1.6 \text{ K}$$

$$\Delta T_{2\times,eq} = 0.9 - 2.8 \text{ K}$$

$$\tau_s = 5 - 9 \text{ yr}$$

$$\tau_1 = 400 - 600 \text{ yr}$$

# SUMMARY & CONCLUSIONS (1)

The *effective heat capacity* of the upper, short-time-constant compartment of the climate system, accounting for other heat sinks, is found to be  $21.8 \pm 2.1 \text{ W yr m}^{-2} \text{ K}^{-1}$  (1  $\sigma$ ).

The *rate of planetary heat uptake is found to be proportional to the increase in global temperature* relative to the beginning of the twentieth century with *heat exchange coefficient*  $1.05 \pm 0.06 \text{ W m}^{-2} \text{ K}^{-1}$  (1  $\sigma$ ).

Transient and equilibrium climate sensitivity were examined for six published forcing data sets having twentieth century forcing ranging from 1.1 to 2.1  $\text{W m}^{-2}$ , spanning much of the range encompassed by the 2007 IPCC assessment.

# SUMMARY & CONCLUSIONS (2)

For five of the six forcing data sets a rather robust linear proportionality is observed between the observed change in global temperature and the forcing, allowing transient sensitivity to be determined as the slope.

*Equilibrium sensitivities* range from 0.24 to 0.75 K (W m<sup>-2</sup>)<sup>-1</sup> (CO<sub>2</sub> doubling temperature 0.88 to 2.75 K), ***less to well less than the IPCC central value*** and estimated uncertainty range for this sensitivity.

Transient sensitivities are less to well less than equilibrium sensitivities.

*Values of sensitivity are strongly anticorrelated with the forcing used to determine sensitivity.*

# SUMMARY & CONCLUSIONS (3)

Improved empirical determination of transient or equilibrium climate sensitivity, and also determination by climate models, *requires uncertainty in aerosol forcing to be greatly reduced.*

Values of the time constant characterizing the response of the *upper ocean* component of the climate system to perturbations range from *4 to 9 years*.

*Transient sensitivity would seem to be more important than equilibrium sensitivity in decisions regarding future CO<sub>2</sub> emissions.*